

- 1. Are you interested in solving puzzles like the one given at the beginning of the lecture? Very interested / A little bit interested / Not interested
- 2. Do you remember what the function \sqrt{n} means? YES / NO

Do you remember what the function $\log_2 n$ means? YES / NO

 \sqrt{n} is the inverse of square: if $y = x^2$, then $x = \sqrt{y}$; e.g., $5 = \sqrt{25}$ because $25 = 5^2$. log₂ n is the inverse of power of 2: if $a = 2^b$, then $b = \log_2 a$; e.g., $5 = \log_2 32$ because $32 = 2^5$.

- 3. What is the value of $\sqrt{64}$? Answer: 8 because $64 = 8^2$ $\log_2 64$? Answer: 6 because $64 = 2^6$
- 4. Do you remember how to expand a polynomial, e.g., (x + 1)(x + 2)? YES / NO

Do you know how to **factorize** a polynomial, e.g., $x^2 + 3x + 2$? **YES** / **NO**

Expanding a polynomial in x, say (ax+b)(cx+d), is to express it in an expanded form without brackets, $(ax+b)(cx+d) = acx^2 + adx + bcx + bd = acx + (ad+bc)x + bd$. For example, expanding (x+1)(x+2) gives $x^2 + 2x + x + 2 = x^2 + 3x + 2$.

Factorizing is the reverse process of expansion, factorizing $acx^2 + (ad + bc)x + bd$ gives (ax + b)(cx + d). For example, factorizing $x^2 + 3x + 2$ gives (x + 1)(x + 2).

5. Try to expand the expression (x+2)(x+3): Answer: $x^2 + 5x + 6$

Try to factorize the polynomial $x^2 + 5x + 6$: Answer: (x + 2)(x + 3)

- 6. Have you learned Mathematical Induction (or Induction simply) before? YES / NO
- 7. Have you heard of the term pseudo code before this lecture? YES / NO
- 8. Try to complete the following **while-loop** to print the value of 2 * i in each iteration up to 20. In other words, your code should output 2, 4, 6, 8, 10, 12, 14, 16, 18, 20.



end

Answer:

```
i = 1
   while i \leq 10 do
   begin
       print 2 * i
       i = i + 1
   \mathbf{end}
Alternatively,
   i=2
   while i \leq 20 do
   begin
       print i
       i = i + 2
       // Note: i = i * 2 is incorrect, only 2, 4, 8, 16 will be printed
   end
The followings are also correct,
   i = 1
   while i < 11 do
   begin
       print 2 * i
       i = i + 1
   end
   i = 2
   while i < 21 do
   begin
       print i
       i=i+2
   end
```

Below are some common mistakes. Find out what will be printed for each of them.

```
i = 2
while i \le 20 do
begin
print 2 * i
i = i + 1
end
i = 0
while i \le 20 do
begin
print i
i = i + 2
end
```