Modeling Judicial Context in Argumentation Frameworks

Adam Wyner and Trevor Bench-Capon

University of Liverpool, Department of Computer Science, Liverpool, United Kingdom

Abstract. Much work using argumentation frameworks treats arguments as entirely abstract, related by a uniform attack relation which always succeeds unless the attacker can itself be defeated. However, this does not seem adequate for legal argumentation. Some proposals have suggested regulating attack relations using preferences or values on arguments and which filter the attack relation, so that, depending on the audience addressed, some attacks fail and so can be removed from the framework. This does not, however, capture a central feature of legal reasoning: how a decision with respect to the same facts and legal reasoning varies as the judicial context varies. Nor does it capture related context dependent features of legal reasoning, such as how an audience can prefer or value an argument, yet be constrained by precedent or authority not to accept it. Nor does it explain how certain types of attack may not be allowed in a particular procedural context. For this reason, evaluation of the status of arguments within a given framework must be allowed to depend not only on the attack relations along with the preference or value of arguments, but also on the nature of the attacks and the context in which they are made. We present a means to represent these features, enabling us to account for a number of factors currently considered to be beyond the remit of formal argumentation frameworks. We give several examples of the use of approach including: appealing a case, overruling a precedent, and rehearing of a case as a civil rather than criminal proceeding.

Keywords. Argumentation, Legal reasoning, Precedent, Precedence, Procedure

Introduction

Since their introduction in [2], abstract Argumentation Frameworks (AF) have provided a fruitful tool for the analysis of the acceptability of arguments in a debate, comprising a set of arguments some of which conflict. In [2], arguments are entirely abstract and related only by a uniform attack relation. This attack relation always succeeds: an argument that is attacked can be accepted only if an argument can be found to defeat its attackers. For some applications, however, such as legal argumentation, which will be...
the focus of this paper, it is useful to allow attacks to fail. Since a court must reach a decision, it requires a rational basis for deciding, for example, between a pair of mutually attacking arguments. For this reason, AFs have been enriched to allow attacks to succeed or fail depending on properties of the arguments involved as in preference-based AF (PAF) of [3] or value-based AF (VAF) of [4]. In effect, the success or failure of the attack is filtered by these properties so that unsuccessful attacks may be removed, and the results of standard AFs applied.

There has been discussion in the literature of how one can justify the exercise of discretion when a court decides between two potentially acceptable but conflicting arguments. We follow the suggestion of [5] and [6] in saying that the decision is made on the basis of a preference for the value promoted by accepting the chosen argument. Such values may be legal principles, such as a conflict between an argument which would promote a “bright line” and one which would promote “flexibility”, or social principles as when one argument would promote equality and another individual freedom. The relation between values and precedents is elaborated in [7]. Thus in the remainder of the paper we assume that a court will choose which argument to accept relative to the court’s ranking over the values which the arguments promote. Thus new decisions reveal the value ranking of the court, and this ranking is used to determine decisions where precedents are followed.

While VAFs accommodate reasoned choice based on legal principles or social purposes, there are other aspects of legal argumentation, in particular, the notions of precedent, precedence, and procedure as found in juridical hierarchies which are not addressed. Precedent here refers to cases which are decided by a court at one point and are subsequently used to guide a decision in another case (upheld) or not (overturned). Precedence refers to the hierarchical relationships between courts; it is reflected in terms of the relationships between legal settings and their effects in determining the decision in a case. Procedure refers to what arguments a court finds legally admissible relative to some proof standard. In some contexts, while a court may be sympathetic to an argument, the court cannot accept it because that court is obliged to follow a previous decision (precedent), or a decision made by a superior court (precedence), or an argument may be legally inadmissible relative to the court’s proof standard (e.g. civil versus criminal proceedings). The nature of the appeals process means that different courts are able to come to different decisions on the same set of arguments. Given these observations, we can see that the evaluation of the status of arguments within a given framework must be allowed to depend not only on the attack relations, nor only on these together with the intrinsic strength of arguments relative to an audience, but also on the ways in which attacks may succeed or fail relative to the contexts and the relationships among contexts in which the arguments and attacks appear. In this paper we will propose a method for accommodating these features using further extensions to AFs.

A set of cases has previously been represented as an AF in [8] and as a VAF in [9]. A means of rewriting VAFs by adding certain auxiliary arguments so that both the object level arguments and meta-level arguments expressing preferences between values are included in the framework [10]. In this paper we describe and exemplify a

\[1\] Where these are not explicitly stated in the judgement, they can be imputed by the analyst.
general approach to address the contextual issues relating to legal argumentation across 
juridical contexts.

The approach has several components. Most generally, it is a static rather than dynamic 
approach in that we provide a structure for the legal system of courts, which we model 
following the description of the system. With respect to this structure, we evaluate 
claims relative to legal contexts which reflect the values of a legal context revealed 
in previous decisions along with precedent, precedence, and procedure. As the legal 
context changes, the outcome changes.

More particular components are:

- We distinguish between object-level arguments and meta-level arguments in 
  argumentation frameworks, where the meta-level arguments represent properties of 
  arguments in the object-level frameworks. Our approach focusses on the meta-level 
  arguments. In a legal context, the object-level arguments are the legal claims while 
  the meta-level arguments are about the claims.
- Each object-level attack relation is represented in terms of a set of meta-level argu-
  ments in a structure of attacks.
- The meta-level arguments are subsorted and the attack relations on them are sub-
  sorted. The attacks represent conceptual relationships among the meta-level argu-
  ments.
- The justification of some meta-level arguments and their relations is based on the 
  object-level arguments and their relations. Other meta-level arguments and their 
  relationships are justified with respect to the judicial system they represent.

In structuring the relations between meta-level arguments, the guiding principle is 
that attacks on other arguments are used to defend certain other arguments against at-
tackers which are weaker in the appropriate respect. We see several examples of this 
below. However, once given the meta-level arguments and their relations, we can ab-
tract from the subsorts of arguments and attacks to reduce the structure to an abstract 
AF. Thus, while our analysis accounts for additional phenomena and adds additional 
machinery, it benefits from the theoretical results and algorithms which apply to AFs 
([11] and [12]).

We distinguish our approach, where we examine argumentation across juridical 
contexts, from argumentation within a juridical context. For instance, [13] focus on 
the dialectical, dialogical, and procedural aspects of arguments for or against a partic-
ular claim within one legal context. They model dialectical argumentation in terms of 
premises, rules, and conclusions along with critical questions. Proof standards and bur-
dens of proof may shift within the legal context among the parties and so contribute 
to determining the outcome of that particular case. In contrast, we take the outcome 
of a dialectical argument within a juridical context as input to our analysis, where we 
consider outcomes as the juridical context changes. In a sense, rather than legal pro-
tagonsists arguing a case before one court, in our analysis, the courts themselves are the 
protagonists. Thus, issues such as premises and critical questions are not directly rel-
vant to our analysis. Furthermore, we abstract over a range of complexities of proof 
standards and burdens of proof in order to focus on the legal admissibility of an argu-
ment. Like [8], we represent a body of case law, not a particular case; it is, then, more 
abstract than [13].
The contributions of the paper are the representation of judicial contexts in an AF, incorporating the central meta-level arguments directly in an AF so that given the AF, one need only reason with respect to the graph. This also implies that the AF has nodes with rich content and the attack relation is fine-tuned to the particular nodes.

The structure of the paper is as follows. Section 1 contains a discussion of relevant aspects of the (English) legal system. In particular, we describe the appeals process, change of use of precedent, and proof standards. A hypothetical working example is presented. In subsequent sections, each of these aspects of the legal system is provided with a graph which is a subgraph of a graph which represents the overall reasoning in the legal system with respect to judicial context. In section 2, argumentation frameworks are outlined, particularly the extension to meta-level arguments, which provide some initial motivation. Section 3 introduces an alternative version of the extended framework, which explicitly introduces additional meta-level elements and relations. With this, we represent object-level arguments and associated values in section 3.1. Section 3.2 presents the appeals process as a case moves through the legal hierarchy. Section 3.3 discusses how precedents are set with respect to values in a structured argument network. Section 3.4 provides our analysis of procedures and proof standards. In section 3.5, we show how we accommodate change in the law relative to social change. This is followed by a brief discussion of temporal aspects relating to precedents in Section 3.5. In section 3.6, the various subgraphs are brought together into the graph which represents reasoning with respect to judicial context. We demonstrate the system with respect to our hypothetical working example. We end with section 4 on related work and observations about opportunities for future work developing our approach.

1 Judicial Contexts

Since the use of precedents varies from legal system to legal system, we need to select a particular legal system to model in this paper. We base our analysis on the English Legal System. Equally, we could have modeled the American or Continental systems; we are not modeling a universal legal system. In this section, therefore, we consider aspects of the English Legal System. Each aspect illustrates how the juridical context can determine the outcome of a case. We have simplified and abstracted over several complexities of the legal system such as the number of courts, their hierarchical relationships, precedent relationships, and other notions of proof standards.

1.1 Appeals Process

The lowest level of the legal hierarchy is the Crown Court, where trials on indictment come before a judge and jury. The evidence, legal arguments, and the decision are given according to the procedures specified for the Crown Court. In particular, the Crown Court is bound by precedents decided by courts higher in the legal hierarchy. The decisions on points of law made in a Crown Court are not binding on any higher level, nor are they binding on other judges in another Crown Court, though they are persuasive. We refer to a ratio decidendi as the legal principle on which the decision is based.
Where there are two (or more) available precedents on which to base a decision, the court chooses which one to follow.

The difference between binding and persuasive precedents is important. A binding precedent is a decided case which a given court must follow in making a decision on the case before it, though this depends on the similarities between the cases. In order to depart from a previous decision, some distinguishing feature or features must be identified between the cases [14]. A persuasive precedent is one which is not binding, but which can be applied should it not conflict with a binding precedent and the court which applies the precedent chooses to do so. Just how a court chooses to follow a precedent (where it can) or to give a different judgement depends on a range of factors which we do not explicitly address since it is another instance of differentiating between two available choices along the lines as discussed in [4] and [9]. For our purposes, we simply assert the status of the precedent (binding or persuasive) and provide the means to reason with either.

Cases decided in the Crown Court may be appealed to a higher level Court of Appeals. Cases can be reconsidered on matters of evidence or of law; for matters of law, there is a claim that the law has been misapplied, the rule of law which was applied is no longer desirable, or some application of the law was inappropriately missed. In effect, the ratio decidendi of the prior decision is somehow faulty.

At appeal, judges do not retry the case, but hear the evidence and arguments. The Court of Appeals can overturn a decision of a Crown Court. While the decisions of a Court of Appeals are binding on Crown Courts, the decisions of a higher court are binding on Courts of Appeals. Moreover, a Court of Appeal is bound by the decision of another Court of Appeal, with a range of exceptions (cf. Young v Bristol Aeroplane Co Ltd [1944] KB 718). Typically a case in the Court of Appeals is heard by three judges.

A case may be appealed from the Court of Appeal to the highest court – the House of Lords. The evidence and arguments are heard again, before five judges, called Law Lords. However, the Law Lords who judge the case are not bound by decisions made at either of the two lower courts. Following Practice Statement [1966] 3 All ER 77, the House of Lords is not even obligated to follow its own previous decisions.2

1.2 Change of Use of Precedent

In general it is considered desirable for decisions made in previous cases to be applied in subsequent cases since this makes for consistency of treatment, a greater certainty as to what the law is, and stability in the system. This is the motivation for the ways in which precedents bind decisions as described above. On occasion, however, social changes may make it desirable that precedents are abandoned. This cannot be done lightly, but it is essential that it be possible if courts are to be able to adapt to changes in society at large. An example is provided by Miliangos v George Frank (Textiles) Ltd [1976] AC 443, where the House of Lords overruled its own previous decision concerning Re United Railways [1961] AC 1007 and in favor of allowing damages to be awarded in a foreign currency. This was in response to a radical change in the exchange rate mechanism that had developed in the interim. Prior to 1966, the House of Lords was

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2 This is one point on which the English system differs from other systems.
bound to follow all its prior decisions under the principle of stare decisis; however, following the Practice Statement [1966] 3 All ER 77, the House of Lords granted itself the right to depart from its previous decisions where it seems right to do so.

1.3 Standards of Proof

Courts may adopt different procedural settings in which to try a case. For our purposes, we consider just civil procedures and criminal procedures. In both settings, evidence must attain a given degree of standard of proof in order to be taken into consideration in the court, where a standard of proof is taken to be a degree of support the evidence has.

In criminal proceedings a very high standard of proof, often expressed as beyond reasonable doubt is required. Depriving a citizen of his liberty is rightly considered a very serious matter, and a person is presumed innocent until guilt is established. This presumption is very strong: it should be maintained if there are any reasonable grounds for doubt. However, civil proceedings, where the victim seeks compensation, uses a lower standard of proof, termed balance of probabilities or preponderance of evidence. This difference means that on the basis of the same facts, some arguments which were rejected as legally inadmissible by the criminal court will be considered and accepted by the civil court. There are a number of examples where the difference between proof standards in different procedural settings is crucial such as cases of rape, murder, and negligence, perhaps the most famous being the O.J. Simpson murder case in 1994. We also consider a proof standard weaker than either of these, scintilla of evidence.3

1.4 A Static Legal System

The legal system as we have described it has both dynamic and static elements: a case “moves” between levels in the judicial hierarchy upon appeal or between procedural contexts; moreover, the legal process is inherently dialogic in the sense that a case is argued by antagonistic sides. However, for our purposes, we focus on the static aspects. At each point in time, where a case is submitted, it is evaluated with respect to a fixed structure; that is, our model represents a post hoc analysis of the effect of the appeal, not the process of appeal. Given a court, the claims, the procedural context, precedents, the proof standards, and evidential status of the claims, we can determine the decision. One would then model the dynamic process as changes over the static model.4

3 While the distinction between proof standards in civil and criminal procedures is clear, proof standards for tribunals are more complex and unclear. As we are addressing judicial hierarchies, we focus on civil cases and assume the proof standard appropriate to civil cases is met.

4 While the appeals process generally involves cases moving upwards the legal hierarchy, cases can also, in effect, move downwards. The term Certiorari is a remedy in which a decision of an inferior court is reviewed by a higher court which can quash the decision and demand a rehearing in the inferior court.
1.5 Pier v. Postson – A Hypothetical Working Example

To make the discussion concrete, we create a hypothetical working example which is based on *Pierson v. Post* (based on [8]). Actual cases present a range of issues and problems from which we abstract in order to present our model of reasoning with judicial context in argumentation frameworks. We call our hypothetical working example *Pier v. Postson*.

For this example, we assume that Pier was pursuing a fox in an uninhabited land though Postson killed and carried off the fox. It is not disputed that Postson knew that Pier was hunting the fox or that Pier knew that Postson was the killer of the fox. We shall call Pier the hunter and Postson the killer. The central issue at stake is who has property rights to the fox – the hunter or the killer? The case is presented before a Crown Court sitting as a civil assembly, which decided in favour of the hunter. The case was appealed to the Court of Appeals on the issue of whether the hunter had acquired property in the fox. The Court of Appeals decided in favour of the killer. The reason given by the majority of the justices was that killing the fox as opposed to hunting the fox supported a bright line in the law, which is an important value in that it promotes peace and order in society. The dissenting minority view was that the case should have been decided for the hunter since the hunter pursued vermin, which is an important value in service to the community.

While the original case of *Pierson v. Post* was not argued on the basis of legal precedents, we want to consider their role in judicial decision making. Therefore, we suppose a hypothetical precedent decided in another Crown Court concerning a case in which a hunter pursued a hawk, which was killed by another, which we call *Wier v. Postal* and which was decided in favour of the hunter rather than the killer, since the value of pursuing vermin was ranked of a greater value than a bright line in the law. We assume that *Wier v. Postal* was not appealed. However, as noted above, precedents set by Crown Courts are persuasive, but not binding on another Crown Court’s decision. So, we presume the Crown Court addressing *Pier v. Postson* was persuaded by the precedent and upheld it. On appeal to the Court of Appeals, the decision by the Crown Court on *Pier v. Postson* is overturned; the precedent by the other Crown Court on *Wier v. Postal* is from an inferior court, so need not be taken into consideration by the Court of Appeals.

In Crown Court, we assume that both Pier’s hunting and Postson’s killing of the fox satisfy the proof standard for Preponderance of Evidence in support of the claim that each possesses the fox, for otherwise, there would be no claim brought before the court. By the same token the Court of Appeals sits as a civil assembly. Consequently, proof standards play no role in this case. A more complex case would either have to involve a civil/criminal distinction or to apply to tribunals, where different proof standards may hold at different levels of the court.

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5 See [15] for a presentation of central issues and a dissenting position on the role of Pierson v. Post in discussions of the law. [15] argues that Pierson v. Post ought to have been considered as a *tort* case, malicious interference with the hunt, rather than a *property* case.

6 In *Pierson v. Post*, the decisions made the choice of values explicit. Often, however, these are implicit and must be attributed through a process of post hoc analysis, as in [9].
Several arguments may have been presented in the original trial, however, what we need to take to the meta-level is the key issue of the case. Analysis of *Pierson v. Post* in [16] identified the difference between the majority and minority opinions as turning only on the value-based resolution of a single pair of arguments. Thus, only these two arguments are represented at the meta-level.

### 2 Argumentation Frameworks and Extensions

We give first an outline of Argumentation Frameworks $\text{AF}$ [2], then discuss how these are expressed with meta-level arguments in [17] and [10]. This sets the main conceptual, formal, and representational elements of our analysis of judicial context in section 3.

An AF comprises objects, relations, and definitions of auxiliary concepts. We take [2] as the most abstract system. In AFs, there is one set of undifferentiated objects, arguments, which can be seen as nodes in a graph; while there is some ambiguity concerning the term argument and the way it is used in the literature, we need not concern ourselves with this here [18]; therefore, to avoid problems, so we prefer to use the terminology of nodes rather than arguments. There is one undifferentiated relationship between the nodes, the attack relation, which can be represented as a graph in which attacks are arcs between nodes representing the arguments.

**Definition 1.** An argumentation framework $\text{AF}$ is a pair $< X, R >$, where $X$ is a set of objects, $\{a_1, a_2, \ldots, a_n\}$ and $R$ is an attack relation between objects. For $(a_i, a_j) \in R$ we say the the object $a_1$ attacks object $a_2$. We assume that no object attacks itself.

The relevant auxiliary definitions are as follows, where $S$ is a subset of $X$:

**Definition 2.** We say that $p \in X$ is acceptable with respect to $S$ if for every $q \in X$ that attacks $p$ there is some $r \in S$ that attacks $q$. A subset, $S$, is conflict-free if no argument in $S$ is attacked by any other argument in $S$. A conflict-free set $S$ is admissible if every $p \in S$ is acceptable to $S$. A preferred extension is a maximal (w.r.t. $\subseteq$) admissible set. The object $p \in X$ is credulously accepted if it is in at least one preferred extension, and sceptically accepted if it is in every preferred extension.

We can represent the AF where $X = \{a_1, a_2\}$ and $R = \{< a_1, a_2 >\}$ as in Figure 1. The preferred extension is $\{a_1\}$ and $a_1$ is sceptically accepted. Figure 2 represents an AF where nodes attack one another – $X = \{a_1, a_2\}$ and $R = \{< a_1, a_2 >, < a_2, a_1 >\}$. In this AF, the preferred extensions are $\{a_1\}$ and $\{a_2\}$, so $a_1$ and $a_2$ are each credulously accepted, and neither are sceptically accepted. Clearly, where $a_1$ and $a_2$ are in an asymmetrical attack, there is only one preferred extension, while where they are in a symmetrical attack, there are two; we use this distinction to model hierarchy, as we shall see.

In Figure 1, nodes are in attack relations. Furthermore, we can make several meta-level statements relative to this AF: $a_1$ defeats $a_2$; $a_1$ is justified; and something defeats $a_2$. The statement $a_1$ defeats $a_2$ expresses a successful attack between specific arguments, which is an attack in which the first argument is not itself attacked and defeated; something defeats $a_2$ is a more general form, where we do not specify just what attacks the second argument. To say that $a_1$ is justified means not only that is it acceptable
with respect to some set of arguments, but expresses why it is acceptable in virtue of the other arguments in that set. These are meta-level statements in that they are statements we make about the nodes \( a_1 \) and \( a_2 \) which represent arguments in the object-level framework.

In addition, we may observe, that classic AFs do not distinguish among sorts of attack relations, nor do they express in virtue of what one node attacks another, just that given the attack relation, one can calculate extensions. The fundamental reason is that where the nodes represent something which is atomic, there can be no explanation for why one node attacks another.

Where the nodes represent more contentful information as is necessary for the representation of judicial context, then we can justify why one node attacks another more specifically. Of course, we may understand intuitively why two statements conflict and so could be represented in an AF attack relation (see a similar discussion in a body of case law in [8]). For example, consider a situation where two individuals \( P \) and \( O \) exchange statements indicated with \( a_1 \) and \( a_2 \) [10, p.241]:

**Dialogue A**

\[P: \text{“Today will be dry in London since the BBC forecast sunshine”} = a_1\]

\[O: \text{“Today will be wet in London since CNN forecast rain”} = a_2\]

The arguments \( a_1 \) and \( a_2 \) are clearly in conflict because of the words dry and wet. The attack between \( a_1 \) and \( a_2 \) is justified since we have a specific intuition about why the content of the nodes are in conflict. We can represent the nodes and attacks as in Figure 2.

In [2], there is no way for an attack itself to be defeated. However, the preferences or values one ascribes to nodes may make attacks unsuccessful [3] and [4]. However, in these approaches, one represents and reasons with preferences and value external to the graph. [17] provides an extension of AFs of [2] to account for preferences or values directly in the AF graph. The analysis is initiated from the notion of attacks on attacks relative to the values of the nodes. For example, our previous dialogue could be continued with:

**Dialogue B (Continues Dialogue A)**

\[P: \text{“But the BBC is more trustworthy than CNN”} = a_3\]
Thus, continuing from the previous dialogue, where $a_1$ attacks $a_2$ and $a_2$ attacks $a_1$, intuitively $a_3$ undermines the attack of $a_2$ on $a_1$ with respect to values (which news source is more trustworthy). We can say that $a_3$ is a higher level attack than the attacks between $a_1$ and $a_2$. The dialogue is represented as in Figure 3.

Formally this is accommodated with an additional sort of attack relation in the AF between a a node and an arc (which represents an attack relation); an attack on an arc (if successful) removes that arc from the determination of node extensions. Following [10, p.242]), we have:

**Definition 3.** An extended argumentation framework $EAF$ is a tuple $< X, R, D >$, where $X$ is a set of objects, $\{a_1, a_2, \ldots, a_n\}$ and $R$ is an attack relation between objects, $R \subseteq X \times X$, and $D$ is an object attacking an attack relation $D \subseteq (X \times R)$. If $(C, (A, B)), (C', (B, A)) \in D$, then $(C, C'), (C', C) \in R$.

Intuitively it is clear from the examples in [17] where an attacking argument, say $a_3$, attacks attack relations between other arguments, say $a_1$ and $a_2$, in virtue of the intuitive content of $a_1$, $a_2$, and $a_3$. However, just what guides such attacks is not formalised, but relies on properties of the nodes; for example, the values in a VAF.

Although it is not our purpose in this paper to formally justify when arguments attack one another, we do rely on the intuitions of attack such as outlined in the Dialogues A and B. This does require that we make the AF less abstract by making use of more explicit information in the nodes.

A move in the direction of less abstract nodes and justified attack relations is made in [10], where the higher level attacks of [17] are rewritten in terms of additional nodes in a structured attack relation, where the additional nodes directly represent meta-level statements. The rewrite is shown to be sound and complete [10] for certain frameworks, in particular, VAFs.

In [10], an AF as graphically represented in Figure 2 is rewritten to an AF as represented in Figure 4, while an extended AF in Figure 3 is represented as in Figure 5. We discuss each of these in turn.

In Figure 4, we have nodes which represent the meta-level statements such as $a_1$ being justified, $a_1$ attacks $a_2$, or $a_1$ is defeated about object-level arguments $a_1$ and $a_2$. In an AF with object-level arguments, the nodes represent only the object-level arguments; in an AF with meta-level arguments, the nodes represent only the meta-level arguments. However, we say the meta-level arguments are about the object-level arguments. More informally and for our legal domain, we call object-level arguments such as $a_1$ and $a_2$ claims and meta-level arguments such as $a_1$ being justified, $a_1$ attacks $a_2$, or $a_1$ is
defeated statements about claims $a_1$ and $a_2$. It is important to keep the object-level and meta-level graphs distinct as it avoids problems of the interpretation of the nodes; that is, if in an AF $a_1$ is a node and $a_1$ is justified is a node, the “levels” would be conflated since $a_1$ is justified contains a node, namely $a_1$.  

In the rewrite in [10], the nodes which express meta-level statements about the object-level arguments are in specified attack relations that represent the content of such attacks on arcs. The node which represents the statement $a_1$ is justified attacks the node Something defeats $a_1$ which attacks $a_1$ defeats $a_2$; in turn, this attacks $a_2$ is justified, which attacks Something defeats $a_2$ which attacks $a_2$ defeats $a_1$. To close the circle, $a_2$ defeats $a_1$ attacks $a_1$ is justified. We have two preferred extensions:

- $\{a_1$ is justified, $a_1$ defeats $a_2$, Something defeats $a_2\}$
- $\{a_2$ is justified, $a_2$ defeats $a_1$, Something defeats $a_1\}$

In both preferred extensions, the elements themselves reflect the concepts otherwise expressed at the meta-level concerning the nodes.

Note that just as in previous AFs, we do not formally express in virtue of what one node attacks another. However, in this extended framework, there is a clear intuitive relationship between the nodes, namely conceptual incompatibility. If a node is justified, then there cannot be some other node which defeats it; if something defeats the given node, then that given node cannot defeat some other node; if one node defeats another node, then the second node cannot be justified. Note as well a statement such as Something defeats $a_1$ does not say what defeats it, just that something does; as we discuss further below, there are a variety of means to defeat a node.

We refer to graphs with a pattern which represents justifications, defeats, and attacks as in Figure 4 as our fundamental structure of attack in an extended framework. To such a fundamental structure, additional structure is added, which changes the justification of nodes.

In the rewrite of [10], an attack on an attack relation is represented as an attack by a node which represents a value ranking on a node which represents the defeat of one argument by another. As such, it represents the VAFs of [4], where the objective was to

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*Fig. 4.* $a_1$ and $a_2$ attack each other

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7 An attractive alternative to allow the representation of both levels in one AF would be to use a natural language referential mechanism of pronominal anaphora. For instance, in a context with a tree one can make a statement about the object “it is tall” without confusion. By the same token, supposing the pronoun $i_1$ refers to the claim $a_1$, $i_1$ is justified would be well-formed without incorporating the object-level. However, we leave this for future work.
use values to determine which of two (or more) preferred extensions are chosen relative to the values of the nodes. Rather than Figure 3 we have Figure 5.

Figure 5 represents an AF where nodes are added to represent statements of value rankings (i.e. \(v_1 > v_2\) and \(v_2 > v_1\)) as well as statements of the audiences which we take to adhere to a value ranking. In [4], audiences are total orderings of values, so an audience can contain some ordering such as \(v_1 > v_2\). The nodes for value rankings and audiences stand in attack relations which indicate which nodes are to remain given successful attacks and to indicate compatibility among the elements: intuitively \(v_1 > v_2\) and \(v_2 > v_1\) attack one another; the audience attacks the value ranking which it does not endorse, which thereby indicates, ceteris paribus, the value ranking it does endorse; the audiences attack one another to reflect the “antagonism” among the audiences and also to maintain the relationship between an audience and an audience’s values.\(^8\)

Given this, we have two preferred extensions which are determined by what nodes are assumed. Assuming an Audience is Y which contains the ordering \(v_2 > v_1\), it attacks \(v_1 > v_2\) and an Audience is X which contains the ordering \(v_1 > v_2\). The remaining value ranking is \(v_2 > v_1\), which is consistent with Audience is Y. In turn, under the assumption that \(a_1\) is associated with value \(v_1\), and \(a_2\) is associated with value \(v_2\), then the node \(v_2 > v_1\) attacks and defeats \(a_1\) defeats \(a_2\). Consequently, \(a_2\) is justified and \(a_2\) defeats \(a_1\) are in the preferred extension, but \(a_1\) is justified not. Thus, one preferred extension is: \{Audience is Y, \(v_2 > v_1\), \(a_2\) is justified, \(a_2\) defeats \(a_1\), Something defeats \(a_1\)\}. The other is calculated similarly. Just as in [4], this framework can differentiate preferred extensions relative to values of nodes and value rankings. This is the meta-level expression of the related value-based framework.

We should emphasise that in [4] audiences are total orders of value rankings. There is, in a sense, some redundancy in Figure 5 where there are both audiences and value rankings. In this paper, we maintain the distinction between audiences and value rankings since in a judicial context the status of an audience may have a bearing on the outcome; that is, two audiences with the same total value ranking may determine different extensions since they interact with other elements of the framework.

In [10], several aspects have been left implicit in the formalisation: the association of nodes with values; the justification of attack relations such as between audiences and value rankings, and value rankings and defeat statements. In [4], these elements are explicit in the formalisation, yet not represented directly in the AF. For our purposes, these are worth making explicit in the AF since they facilitate representation and reasoning in an AF of judicial context.

In the extensions to the value-based approaches, the core idea is to add nodes in structured attack relations which lead to preferred extensions that contain information about the claims (i.e. \(a_1\) and \(a_2\)), namely whether they are justified, whether they are defeated, and which node defeats them. In Figure 5, the value ranking node attacks a node of the fundamental structure of attack, and in virtue of this, we change the outcome. We view the value ranking mechanism as a subgraph of the overall AF graph of which it is a part in that by adding or removing it, we can relativise the outcome of the preferred extensions of the fundamental structure of attack.

\(^8\) This does not preclude modes with richer structures of audiences and values.
In the following section our approach to judicial contexts is an elaboration of this approach of adding meta-level information in structured attack relations as subgraphs of a graph which includes the fundamental structure of attack.

We have discussed two ways to develop AFs – extended AFs and meta-level statements. While some extended AFs cannot be rewritten in terms of meta-level statements, those which we require can be [10], and we prefer this approach as it allows the use of standard AF semantics.

3 Representing Legal Context

In this section, we develop and articulate ideas of extended argumentation frameworks to provide an analysis of judicial context in an argumentation framework. Our goal is a graph which represents judicial context such that given decisions of a level of court (the audience), procedure (criminal or civil), precedent (if any), value ranking, values of claims, and standard of proof of the claims, we can determine which claims are justified. This final graph is presented in Figure 12 in section 3.6. To justify and illustrate each of the components, over the course of the subsections below, we decompose this graph into several subgraphs each of which represents one component of legal reasoning in judicial contexts.

Our general strategy is to add a subgraph (some structure of nodes in attack relations) of which some nodes attack nodes of some other subgraph; the example is nodes of the subgraph of audiences and value-rankings attacking nodes of the fundamental structure of attack in Figure 5. However, one additional aspect is that we build subgraphs with some intermediate structure: we determine the base-level nodes which then combine into intermediate nodes, which may interact with other intermediate nodes, ultimately leading to attacks on nodes of some other subgraph.

In section 1, we introduced a variety of issues related to judicial contexts. We looked at how the values of a court majority determine the outcome of a legal decision. We then considered precedence relations, where decisions by higher courts trump decisions by lower courts (lex superiori). We discussed precedents. Finally, we had an overview of
issues related to *standards of proof*. For each of these issues, we introduce and discuss a subgraph. Note that we do not consider the merits of the claims; our concern is how they have been received by the various assemblies. Moreover, we only discuss a single conflict: in a body of case law, there are usually several related conflicts.

In the following subsections, we present a series of *subgraphs* of an overall graph of an AF, which appears in section 3.6; each of the subgraphs is explained and exemplified so the complex final graph can be understood. Our approach is to have nodes that represent atomic and complex expressions in specified attack relations; the complex expressions are justified in virtue of the atomic expressions. We create the space of possible nodes and attack relations (a selection from the logical space of possible nodes and attacks in consideration of space); given choices in this space with respect to atomic expressions, we can calculate the resultant preferred extension.

We begin with a reconstruction of [10], discussed with respect to Figure 5, making explicit the association of nodes with values. Following in this vein, we connect the output nodes to our fundamental structure of attack. We call this the *Arguments and Values* subgraph, and it highlights some of the key moves in composing the subgraphs. Then we turn to our analysis of precedence in judicial hierarchies along with values. This is presented in two stages: the construction of contexts and value rankings; the relationship between value rankings and valued claims.\footnote{Recall that value rankings are determined in our *ex post* analysis and may not have been explicit in the decisions.} We refer to this as the *Precedence* subgraph. Nodes of the Precedence subgraph are connected to nodes of the Arguments and Values subgraph. With this, we can calculate preferred extensions of justified nodes relative to contexts and values. We introduce precedents in the *Precedents* subgraph, showing how precedents can effect a current case relative to the court hierarchy and value ranking. Finally, procedural contexts and standards of proof are introduced in the *Proof Standards* subgraph. Additional topics bearing on development of case law through a sequence of decisions are discussed.

### 3.1 Arguments and Values Subgraph

In this subgraph, nodes are associated with values along with value rankings. Given such associations, nodes are then used to attack nodes of the fundamental structure of attack. This is, in effect, simply an elaboration of Figure 5. We simplify here and assume that our claims $a_1$ and $a_2$ can have values $v_1$ or $v_2$, but the claims cannot both have the same value; we could have further articulated the graph to represent associations of individual claims and particular values, but it would lead to more of a graph than is needed. Furthermore, the value rankings are a strict ordering. Note again for clarity that what represented arguments (i.e. nodes) $a_1$ and $a_2$ in [2] and [17] are *claims* in our presentation. About claims one can make *statements* such as $a_1$ has $v_1$, where $v_1$ is a value. Statements here are the *nodes* of the AF.

In Figure 6, we form complex expressions from the values that claims have and the value rankings: if an extension has the node for $a_1$ has $v_1$, and $a_2$ has $v_2$ along with the node for $v_1 > v_2$, then the extension has the node $a_1$ has $v_1$, $a_2$ has $v_2$, and $v_1 > v_2$. Furthermore, the attack relations are intuitively obvious: $v_2 > v_1$ attacks $a_1$.
has $v_1$, $a_2$ has $v_2$, and $v_1 > v_2$ since the values are in conflict. By the same token, the complex expressions attack statements which are incompatible with them. While there is a degree of redundancy in this, having such distinct nodes facilitates the analysis (see discussions of intermediate concepts [19], [20], [21], and [16]).

Now we are in a position to consider the impact of this latter node, $a_1$ has $v_1$, $a_2$ has $v_2$, and $v_1 > v_2$, with respect to the fundamental structure of attack. Rather than putting the calculation of defeat of a claim relative to values of claims and value rankings in the meta-theory, we directly incorporate into the AF those nodes which represent values of claims and value rankings. For example, in Figure 7, the node $a_1$ has $v_1$, $a_2$ has $v_2$, and $v_1 > v_2$ which represents the values of the claim and the value ranking attacks the node $a_2$ defeats $a_1$. We use this notion of attack relative to value rankings for simplicity. By comparison, in [4], a node $a_1$ defeats another node $a_2$ in the graph only if the value of $a_1$ has an equal or higher value on the value ranking than the value of $a_2$; if so, then it is justified to claim that $a_1$ defeats $a_2$, and conversely it is not justified that $a_2$ defeats $a_1$. This is the reason why a node representing $a_1$ has $v_1$, $a_2$ has $v_2$, and $v_1 > v_2$ attacks the node $a_2$ defeats $a_1$, but leaves $a_1$ defeats $a_2$. Similar reasoning applies to the other attacks. Note that the attacks here are not symmetrical, for the complex expression implies the defeat statement which is eliminated and not vice versa.

Note that we have two subgraphs Figure 6 and Figure 7 of a larger graph. The larger graph is broken into parts for ease of presentation; where one finds the same nodes in two (or more) graphs, it is to be assumed that these are in fact the same node and the graph can be redrawn to reflect this. As mentioned earlier, all the subgraphs are composed into one graph in Figure 12.
If we just consider the four nodes (i.e. ignoring the intermediate nodes) \( a_1 \) has \( v_1 \) and \( a_2 \) has \( v_2 \), \( a_2 \) has \( v_1 \) and \( a_1 \) has \( v_2 \), \( v_1 > v_2 \), and \( v_2 > v_1 \), these give rise to four preferred extensions with respect to the justified claim.

- \{ \( a_1 \) has \( v_1 \) and \( a_2 \) has \( v_2 \), \( v_1 > v_2 \), \( a_1 \) is justified \}
- \{ \( a_1 \) has \( v_1 \) and \( a_2 \) has \( v_2 \), \( v_2 > v_1 \), \( a_2 \) is justified \}
- \{ \( a_2 \) has \( v_1 \) and \( a_1 \) has \( v_2 \), \( v_1 > v_2 \), \( a_2 \) is justified \}
- \{ \( a_2 \) has \( v_1 \) and \( a_1 \) has \( v_2 \), \( v_2 > v_1 \), \( a_1 \) is justified \}

This shows that where we want the result to be just one justified claim, we must determine both the values of claims and value rankings; fixing only one will result in two preferred extensions each with a different justified claim.

### 3.2 Precedence Subgraph

One aspect of judicial decision making is the imposition of value rankings relative to a legal context in determining the outcome. For the moment, we assume there are no precedents so that every case is decided on its merits relative to the value ranking of the court in which the case is made. While a decision may be decided either way prior to being argued in a legal context, the role of the courts is to decide one way or the other, though this may be overturned later on appeal. While we may assume Figure 5 represents arbitrary audiences and their correlated value rankings, we want to associate judicial contexts with value rankings such that only the value ranking of the given judicial context is active in determining the outcome of the decision. If the case is presented before a Crown Court, then the value ranking of that court ought to predominate over the value ranking which represents some non-judicial audience; if the case is presented before the House of Lords, then the House of Lords value ranking ought to predominate.

In terms of the AF, precedence relations between courts appears as the imposition of the value ranking of the superior court on the inferior court; the value ranking of a superior court which yields a particular decision must be adopted by the inferior courts.
but not vice versa. In terms of the graph, we want an extension in which appears not only the court making the decision, but also all courts lower in the judicial hierarchy which also have the same value ranking. From this extension, we want to exclude all courts higher in the hierarchy than the one making the decision as well as all courts with other value rankings.

We have independent representations of attacks between court levels as well as between value rankings; we then have complex expressions that represent the value rankings associated with particular court levels, using courts and value rankings to attack these complex expressions. Following our previous observation, we distinguish value rankings from audiences: different audiences may have the same value ranking, but be distinct in other respects (importantly with respect to precedent).

With respect to Figure 8, the attack relations between statements with values are obvious. The attack relations between courts is interesting for it reflects a conceptual incompatibility, not a logical incompatibility; the legal system is defined in such a way that no court can both sit at a Crown Court and a Court of Appeals (similarly for the other pairs). In terms of ontologies, we say the courts are disjoint; in lexical semantics [22] a range of oppositional terms are observed such as master-slave or teacher-pupil. Furthermore, note the distinct attack relations between court levels and statements of values of a court, where, for example, Crown Court attacks both $v_1 > v_2$ in Court of Appeals and $v_1 > v_2$ in House of Lords, while Court of Appeals attacks $v_1 > v_2$ in House of Lords. The lower court eliminates the higher courts from consideration. Though this is perhaps counterintuitive, it reflects the imposition of the value ranking of higher courts on lower courts, as discussed above and exemplified below.

With respect to Figure 8, consider the two following examples. Suppose an undecided case is submitted to a Crown Court and the value ranking of that court are $v_1 > v_2$, the preferred extension is:

\{Crown Court, v_1 > v_2, v_1 > v_2 in Crown Court\}

In this, nothing is justified concerning the values of superior courts; $v_1 > v_2$ is sceptically accepted and only with respect to one court level, the Crown Court. In contrast, if the same case were to be submitted directly to the House of Lords and the values of the court were $v_1 > v_2$, then we have three preferred extensions:

- \{House of Lords, v_1 > v_2, v_1 > v_2 in House of Lords\}
- \{House of Lords, v_1 > v_2, v_1 > v_2 in Court of Appeals\}
- \{House of Lords, v_1 > v_2, v_1 > v_2 in Crown Court\}

Here the value ranking $v_1 > v_2$ is sceptically accepted and with respect to every level of court. In other words, a decision in the House of Lords along with its value ranking justifies that the House of Lords’ value ranking holds in subordinate courts as well. By the same token, a decision in the Court of Appeals justifies the value ranking in both Courts of Appeals and Crown Courts, but does not justify the value ranking in the House of Lords.

The judicial hierarchy is expressed in terms of how higher courts determine the value ranking that hold of lower courts, but not vice versa; in other words, it reflects the power of which court decides a question set to the legal system.
In Figure 9, we connect the values of courts in Figure 8 with the values of claims and value rankings in Figure 6 and then with the fundamental structure of attack in Figure 4. Since Figure 7 gives us the justifications of claims given values of claims and value rankings, we can justify the claims relative to judicial context and value rankings in a judicial hierarchy using Figure 9. It is worth noting that once the claims are assigned values and the value ranking is determined, the particular court has little substantive effect on determining the justified claim since these are already determined by the values on claims and the value ranking. What is significant is the “spreading” effect on value rankings among the courts, which is novel. In addition, the role of the subgraph on courts and values is more significant when we consider interactions between a current court and precedents.

As one picks courts, value rankings, and values of claims, the preferred extensions are determined which express the justifications of the claims \( a_1 \) and \( a_2 \). For example, suppose the court is a Crown Court, where the value ranking is \( v_1 > v_2 \), \( a_1 \) has \( v_1 \), and \( a_2 \) has \( v_2 \). For clarity, we have left out some of the intermediate nodes, which are easily calculated.

\[
\{\text{Crown Court, } v_1 > v_2, v_1 > v_2 \text{ in Crown Court, } \ a_1 \text{ has } v_1 \text{ and } a_2 \text{ has } v_2, a_1 \text{ defeats } a_2, a_1 \text{ is justified}\}
\]

The point here is that the Crown Court does not impose its value ranking on the other levels of the judicial hierarchy, which are underdetermined.

In contrast, if the court is the House of Lords, where the value ranking is \( v_2 > v_1 \), \( a_1 \) has \( v_1 \), and \( a_2 \) has \( v_2 \), then the preferred extension is:
Here we see that the House of Lords does determine the value ranking for the other courts in the judicial hierarchy, which must all be consistent with the value ranking of the House of Lords.

We claim this models the appeals process in a judicial hierarchy, for as the case passes through the judicial hierarchy, the case is decided by the court and imposed on courts lower in the judicial hierarchy. There is an important note to emphasise in this process: the ascription of values to the claims at the court of first instance must be maintained as the case is appealed. Otherwise, as we saw at the end of section 3.1, the justified claim varies according to the values on claims and the value ranking; however, we want only the value ranking to vary the justified claim. This is consistent with legal practice, where the court of first instance fixes the facts which are maintained throughout the appeals process. We can ensure this since we are analysing completed cases, not modeling them while they are happening.

3.3 Precedents Subgraph

To this point, we have represented the hierarchical relationships between the courts and the bearing of values claims and value rankings on the justification of claims. However, it is an “atemporal” representation of a current case: every change of judicial context can change the outcome, but interactions between precedents and judicial context play no role. In order for precedent to play a role, it must be capable of changing the outcome of the current case for that which would otherwise follow. We follow a logic similar to
previous graphs: we assume that the values of a precedent case of a higher court filter the values of lower courts in the current case by eliminating those courts and values.

In the following, we assume an eight-place relation which stands for an intermediate concept **Precedent** which is defined with the following set of elements. There is a set of judicial contexts \{Crown Court, Court of Appeals, House of Lords\}, a set of value rankings, a set of claims \{a_1,...,a_n\}, a set of similarity statements, and a set of claim value statements. Judicial contexts, value rankings, and claims are familiar from above.

The claim value statements are of the form \(a_i \ has \ v_j\) as before. The similarity statements are of the form \(a_i \approx a_j\), where \(a_i\) and \(a_j\) are claims from among the set of claims; it is a similarity statement in that the arguments \(a_i\) and \(a_j\) are similar as determined by case-based reasoning ([23], [24]). This is the expression which makes the precedent relevant to the current case. How a particular precedent is determined to apply relative to a current case is not crucial; we can assume that case-based reasoning locates an appropriate precedent and applies it to the case at hand, assuming some means to make such a case-based comparison.

With this, \(\text{Precedent} \subseteq (\text{judicial contexts} \times \text{value rankings} \times \text{claims} \times \text{claims} \times \text{similarity statement} \times \text{similarity statement} \times \text{claim value} \times \text{claim value})\). In Figure 10, we illustrate a subgraph with three example precedents.

- **Precedent(Crown Court, \(v_1 > v_2, a_3, a_4, a_3 \approx a_1, a_4 \approx a_2, a_3 \ has \ v_1, a_4 \ has \ v_2\))**
- **Precedent(Court of Appeals, \(v_2 > v_1, a_5, a_6, a_5 \approx a_1, a_6 \approx a_2, a_5 \ has \ v_1, a_6 \ has \ v_2\))**
- **Precedent(House of Lords, \(v_1 > v_2, a_7, a_8, a_7 \approx a_1, a_8 \approx a_2, a_7 \ has \ v_1, a_8 \ has \ v_2\))**

The first represents a precedent made in Crown Court where the value ranking was \(v_1 > v_2\), where the decision concerned two claims \(a_3\) and \(a_4\) which were in conflict and bore the values \(v_1\) and \(v_2\) respectively. These claims are respectively similar to \(a_1\) and \(a_2\). The decision is given by the court according to the value ranking and values of the claims: \(a_3\) is justified and \(a_4\) is not justified. Similar points can be made about the other examples. While a more complex graph could be provided to represent precedents, it is more straightforward for our purposes to provide this high-level intermediate concept. The subgraph in Figure 10 relates to the subgraph in Figure 8 with respect to value rankings and judicial contexts.

Notice here that we have a series of precedents that all may bear on \(a_1\) and \(a_2\), made in different courts and with different value rankings. In effect, we can consider that a decision made in a Crown Court in Precedent 1 is overturned in a Court of Appeals, which is again overturned in the House of Lords, thereby upholding the initial precedent. However, only in section 3.5 do we discuss temporal aspects of precedent. Yet, in Figure 10, we represent with the attack relation the relationships between these precedents in virtue of the judicial hierarchy: a precedent set by the House of Lords trumps a precedent set by the Court of Appeals, which trumps a precedent set by the Crown Court.

Along with this representation of precedent, the precedent attacks the other relevant nodes with which it conflicts. First, we consider attacks of precedents on value rankings. In Figure 10, **Precedent(Crown Court, \(v_1 > v_2, a_3, a_4, a_3 \approx a_1, a_4 \approx a_2, a_3 \ has \ v_1, a_4 \ has \ v_2\))** asymmetrically attacks the node representing \(v_2 > v_1\). Without this attack, the precedent could not determine the outcome of the current case; in effect, this attack
allows the precedent to impose its value ranking on the judicial system. However, if the precedent is itself attacked, then the attack of the precedent on the value ranking fails and the precedent does not impose its value ranking, which is otherwise be chosen by the court which is deciding the case.

Next, consider the attacks between precedents and current judicial contexts (court value rankings such as nodes $v_2 > v_1$ in Crown Court). There are two parameters to consider: the comparative value rankings and the comparative roles of the court in the judicial hierarchy. Note that it is not always the case that where the value rankings between precedents are different than the current judicial context, the nodes attack one another, for the attack is conditioned on the comparative roles of the courts in the judicial hierarchy. These formally represent the differences between 

persuasive
and

binding

precedents in judicial contexts. We have the following examples:

- Precedent(Crown Court, $v_1 > v_2$, $a_3$, $a_4$, $a_3 \approx a_1$, $a_4 \approx a_2$, $a_3$ has $v_1$, $a_4$ has $v_2$) attacks and is attacked by $v_2 > v_1$ in Crown Court
- Precedent(Crown Court, $v_1 > v_2$, $a_3$, $a_4$, $a_3 \approx a_1$, $a_4 \approx a_2$, $a_3$ has $v_1$, $a_4$ has $v_2$) is attacked by $v_2 > v_1$ in Crown Court
- Precedent(Court of Appeals, $v_2 > v_1$, $a_5$, $a_6$, $a_5 \approx a_1$, $a_6 \approx a_2$, $a_5$ has $v_1$, $a_6$ has $v_2$) attacks $v_1 > v_2$ in Court of Appeals

In the first example, a precedent set in a Crown Court is persuasive on another Crown Court; the current case can be decided either according to value ranking of the precedent or the value ranking of the current court. How a current court decides which to follow is (presumably) another “higher” layer of value judgement. In the second example, a precedent set in a Crown Court is not binding or persuasive on a Court of Appeals; that is, the current court is free to decide the case (i.e. decide the value ranking) as it sees fit (though this might be to uphold the precedent). In the third example, a precedent set by a Court of Appeals is binding on a Court of Appeals; the current court must abide by a decision made by another Court of Appeals, for where such a precedent holds, the current court cannot decide contrary to the value ranking established in the precedent. In these examples, we see that the attacks are determined according to the roles of the courts in the judicial hierarchy and their relationships.

In general in the English Legal system, precedents set in a higher level court asymmetrically attack precedents set in a lower level court. Precedents set in a higher level court asymmetrically attack current courts at a lower level. A higher level current court attacks a lower level precedent. Attacks between a precedent set in courts of the same level as the current court are sometimes symmetrical (e.g. Crown Court and House of Lords), but sometimes asymmetrical (Court of Appeals). As such symmetrical attacks give rise to two (or more) preferred extensions, these indicate discretion to follow or reject the precedent. We assume some other means to guide the discretion, for example, some additional value ranking in the current court. The logic of the relationships is that precedents and judicial hierarchy interact to eliminate assertions of value rankings according to the relative strength of the current court or precedent in the judicial hierarchy. In light of this, where there is a precedent, we cannot determine the value ranking until the effect of the precedent in the court context has been evaluated. Finally, we assume that where a statement is not indicated in terms of the Precedent relation
Suppose that we only have the precedent which is set in a Crown Court (thus there are no other precedents in the graph). In this precedent, $a_3$ is justified and $a_4$ is not justified given the values of the claims and the value ranking of the court. We assume that $a_1$ has value $v_1$ and $a_2$ has value $v_2$. The case is taken to a Crown Court, which has value ranking $v_1 > v_2$. As the precedent and the current court attack one another, we have two preferred extensions. If the current Crown Court accepts the values of the precedent (so $v_1 > v_2$ in Crown Court appears in the extension) and so upholds the precedent, then the precedent attacks $v_2 > v_1$ in Crown Court, $v_2 > v_1$ in Court of Appeals, and $v_2 > v_1$ in House of Lords, as well as $v_2 > v_1$. With reference to Figure 8, the current Crown Court defeats all the nodes with Court of Appeals and House of Lords.

Fig. 10. Precedent in the Judicial Hierarchy
Lords. With reference to Figure 9, the value ranking and judicial context are: $v_1 > v_2$.

$v_1 > v_2$ in Crown Court. Consequently, $a_1$ is justified in the preferred extension (among other elements).

The case has been appealed to the Court of Appeals, where (suppose) the value ranking is $v_2 > v_1$, and we have assumed that on appeal the values of claims are maintained, so $a_1$ has $v_1$, and claim $a_2$ has $v_2$. If the value ranking of the precedent held, then similar to the precedent case, the decision in the current case would be that $a_1$ is justified. However, the court level and its value ranking attack the precedent from the Crown Court. Thus, the decision is overturned in the current case in the Court of Appeals so that $a_2$ is justified.

In these two examples, the current court has, in effect, a choice of value ranking to follow. Consider a different scenario in which the current court has no choice to follow its own value ranking. Suppose the only precedent is Precedent(Court of Appeals, $v_2 > v_1$, $a_5$, $a_6$, $a_5 \approx a_1$, $a_6 \approx a_2$, $a_5$ has $v_1$, $a_6$ has $v_2$) attacks $v_1 > v_2$ in Court of Appeals, and the current court is a Court of Appeals with value ranking is $v_1 > v_2$. The claims and values are: $a_1$ has $v_1$, and claim $a_2$ has $v_2$. In this scenario, if there were no precedent or a precedent in line with the value ranking of the current case, then $a_1$ is justified would be in the preferred extension. However, the precedent does hold and asymmetrically attacks $v_1 > v_2$ in Court of Appeals and the value ranking $v_1 > v_2$. Consequently, $v_2 > v_1$ in Court of Appeals and the value ranking $v_2 > v_1$ are in the extension, from which it follows that $a_2$ is justified in the preferred extension. In this instance, the Court of Appeals is bound to follow a precedent, though this is not in keeping with its own value ranking.

In this way, we account for the the appeals process relative to precedent and precedence.

### 3.4 Proof Standards Subgraph

In this section, we discuss and represent the conditions of legal admissibility under different types of procedure and relative to standards of proof that the claim supports. A claim which is admitted into the framework will satisfy a particular proof standard (PS) with respect to the case under consideration.

For our presentation, we abstract over the relationship between proof standards and burdens of proof (see [13]). While [13] discuss four levels of PS arranged in a hierarchy from lower to higher, we discuss only three. Just as we have associated claims with values, we also associate a claim with the proof standard it satisfies. We are not representing that which determines whether a particular claim satisfies a given proof standard. For example, in the O.J. Simpson murder trial, a criminal court did not decide that Simpson murdered his ex-wife Nicole Brown Simpson and her friend Ronald Goldman in 1994 since the requisite standard of proof, Beyond Reasonable Doubt, was not shown to hold between the evidence and the claim. However, given the same evidence and legal arguments, a civil court decided that Simpson was guilty of their wrongful deaths; in this case, the requisite weaker standard of proof, Preponderance of Evidence, was met to support the claim. In the same vein, we are considering just whether the claim meets the requisite proof standard, not how the proof standard is determined. We refer to the proof standard on a claim as the claim’s evidential status. However, we
presume proof standards can be accommodated to notions of AF as below:10 In Figure 11, we indicate the proof standard on a claim such as a₂ with a₂ has Scintilla, a₂ has Preponderance of Evidence, and a₂ has Beyond Reasonable Doubt.

- Scintilla of Evidence (S): the evidence is credulously accepted, meaning that there is at least one preferred extension in which the evidence holds. The evidence has some support, but support does not necessarily outweigh attacks.
- Preponderance of Evidence (PE): the evidence is accepted in the majority of preferred extensions. The support for the evidence outweighs attacks on it.
- Beyond Reasonable Doubt (BRD): the evidence is sceptically accepted, meaning that the evidence holds in every preferred extension. There is no successful attack on the evidence.

The preferred extensions referred to in these bullets are those that are generated from the AF used by the court in making the original decision at the object-level. At the object-level, the argument may have been skeptically acceptable or credulously acceptable; thus, we now take up to the meta-level not only that the argument was justified, but also the standard of proof in respect of which it was justified.

Under different procedures, different proof standards are used to determine whether a claim is legally admissible under that procedure: where no judicial proceedings apply (as in an informal discussion), S may be sufficient, while in civil proceedings, at least PE is required, and in criminal proceedings BRD is required. In Figure 11, these procedural contexts are represented as Procedure is Informal, Procedure is Civil, and Procedure is Criminal.

We are interested to represent the relationship between a given evidential status of a particular claim, the procedural context, and the admissibility of the claim relative to the proof standard and procedural context. Where the evidential status of the claim is not sufficient with respect to the procedural context, then that claim is inadmissible and so cannot be justified; if the node which represents inadmissibility is eliminated, then the claim is admissible (but not necessarily justified).

In our representation, we have nodes that represent inadmissibility of a claim in different procedural contexts; the inadmissibility nodes attack the node that represents that the claim is justified. Where this attack fails, the claim is admissible. We have nodes that represent the different proof standards associated with the claim. If a claim has only S, then it is inadmissible under both civil and criminal procedures; thus, the node which represents the claim bearing this proof standard does not attack either nodes for inadmissibility. If an argument has PE, then the node attacks inadmissibility under a civil procedure in which instance, the claim is admissible under that procedure and potentially justified. However, it is not admissible under a criminal procedure, so if the court sits as a criminal court, the argument is inadmissible. Finally, if the argument has BRD, then it is admissible under either civil or criminal procedures.

Note the asymmetrical relationships between S, PE, and BRD: if the argument only has S, then it does not also have PE and BRD. Therefore, neither of the inadmissibility nodes are eliminated. If a claim only has PE, then it eliminates BRD; it is admissible

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10 We are abstracting over the relationship between supporting evidence and proof standards as well as the analysis in AFs, which are substantive topics for future research.
under civil procedure, but not under criminal procedure. A claim which has PE is also compatible with S. On the other hand, if a claim has BRD, it is admissible whether under civil or criminal procedures, which is compatible with S and PE.

At this point, we can turn to fixing the procedural context. The informal procedure eliminates inadmissibility under both civil and criminal procedures since there is no applicable notion of admissibility; in other words, in an informal context, any claim is admissible, though not necessarily justified. The Civil context eliminates inadmissibility under criminal procedure. The Criminal context eliminates the civil procedure. Note that the contexts attack one another since they are mutually incompatible.

It is the combination of the evidential status of the claim along with the context that determines whether the claim is inadmissible relative to the procedural context. For example, if the context is informal and the claim has BRD, the claim is (potentially) justified; if the context is civil and the claim has BRD, the claim is (potentially) justified under a civil procedure; if the context is criminal and the argument has PE, the claim is not justified since a claim with PE is not admissible under a criminal procedure.

3.5 Additional Topics

In this section, we briefly outline how changes in law and temporal aspects of precedents.

Change in Law The relationships between the courts in the judicial hierarchy allow that Crown Courts and the House of Lords may overturn a legal precedent (at the appropriate level of the courts in the judicial hierarchy), which signifies a change in the law. In the representation in Figure 10, precedent cases and current cases in Crown Courts and the House of Lords (separately) attack one another. Consequently, in each instance, there are two preferred extensions, one with the precedent and one with the current case. How a decision is reached as a choice between these two extensions may be determined by yet another value selection such as initially motivated VAFs [9].

![Fig. 11. Proof Standards and Procedural Context](image-url)
could introduce this meta-level structure directly, but it adds little of substance to the approach, so we leave it aside here.

**Temporal Aspects of Precedents** An important aspect of reasoning with precedents ([25], [26], and [27]) is that decisions occur as a temporal sequence. Later cases may colour the interpretation of concepts used in earlier cases. In this model, a concept is introduced, goes through a period of instability as its meaning is refined through decision, followed by a period of stability where it is routinely applied, and finally falls out of favour when it fails to be adequate to the changed social circumstances. The introduction and rejection of concepts tend to be marked by landmark cases such as the *Estus case* in US bankruptcy law ([27]). As is clear from [26], the general effect of this evolution is that where precedents are in conflict (through explicit overruling, implicit overruling, rejection or modification of the *ratio decidendi*) the more recent decision is the one that is followed.

In terms of our approach, this is straightforwardly accommodated. We suppose precedents can be compared in terms of claims and values, so we are only interested in precedents in which the cases are relevant (similar claims which have the same values as the current case), but the value ranking between the precedents is different (so there is a conflict between the precedents); consequently, each precedent would justify a different claim in the current case. Finally, we introduce an additional *temporal* parameter into the precedents such as $t = 02-10-1995$, meaning that the case was decided on 02-10-1995. Finally, we assume that temporally later precedents asymmetrically attack temporally earlier precedents. Thus, a more recent precedent eliminates an older precedent.

For instance, suppose Precedent(Crown Court, $v_1 > v_2$, $a_1$, $a_2$), $b_1$ has $v_1$, $b_2$ has $v_1$, $t = 02-10-1995$ and Precedent(Crown Court, $v_2 > v_1$, $c_1$, $c_2$, $c_1$ has $v_1$, $c_2$ has $v_2$, $t = 05-11-1960$). Both serve as precedents for a current case involving $a_3$ and $a_4$; they show opposing value rankings $v_1 > v_2$ and $v_2 > v_1$, so they can be understood to attack one another. However, given our temporal condition, the precedent dated 05-11-1960 asymmetrically attacks and defeats the precedent dated 02-10-1995.

### 3.6 An Integrated Graph with Pier v. Postson

In the following, we discuss our hypothetical case *Pier v. Postson* as it is appealed from a Crown Court to a Court of Appeals where there is only one precedent (*Pier v. Postson*) (which simplifies the graph somewhat) and the values associated with the claims have been fixed. We evaluate the case with respect to Figure 12, which is a graph (simplified where possible) which integrates all the subgraphs we have discussed before.

In the precedent *Wier v. Postal*, a decision was made in a Crown Court for the hunter ($a_3$, which means the hunter is entitled to possess), against the killer ($a_4$, which means the killer was entitled to possess), and the values are pursuing vermin ($v_1$) and a bright line in the law ($v_2$), where $v_1 > v_2$. This implies that $a_3$ has $v_1$ and $a_4$ has $v_2$. The claim $a_3$ is justified in the precedent.

Precedent(Crown Court, $v_1 > v_2$, $a_3$, $a_4$, $a_3$ has $v_1$, $a_4$ has $v_2$)
The case of *Pier v. Postson* is brought before a Crown Court sitting as a civil court where a decision for the hunter is \(a_1\) (the hunter is entitled to possess) and a decision for the killer is \(a_2\) (the killer is entitled to possess). These decisions are associated with values, where \(a_1\) has \(v_1\) and \(a_2\) has \(v_2\). The current Crown Court is not bound by the precedent, which means that the current Crown Court can set its value ranking as either \(v_1 > v_2\) or \(v_2 > v_1\). We assume it sets the value ranking to \(v_1 > v_2\) (suppose it has a high value on being conservative). Finally, we assume that both Pier’s pursuit of the fox and Postson’s killing of the fox meet that proof standard of Preponderance of Evidence in support of either decision, which passes the requisite proof standard for a civil procedure (for simplicity the Figure 12 shows on admissibility for \(a_2\), which is similar for \(a_1\)). Therefore, admissibility does not rule out one or the other claim.

As we can see, the current Crown Court upholds the decision of the precedent set by a Crown Court and decides for the hunter since \(a_1\) is justified. The preferred extension is (leaving out some intermediate nodes):

\[
\{\text{Crown Court, } v_1 > v_2, a_1 \text{ has } v_2, a_1 \text{ has Preponderance of Evidence, } a_2 \text{ has Preponderance of Evidence, Civil Procedure, } a_1 \text{ defeats } a_2, \text{ Something defeats } a_2, a_1 \text{ is justified.}\}
\]

Subsequently, the case is appealed to a Court of Appeals. At the Court of Appeals, the value rankings could again go either way. However, the Court of Appeals decides in favour of the killer using the value ranking of \(v_2 > v_1\) (presumably the court has “progressive” views on hunting). In addition, the precedent set in a Crown Court is overruled. Therefore, the preferred extension is:

\[
\{\text{Precedent(Crown Court, } v_1 > v_2, a_3 \approx a_1, a_4 \approx a_2, a_3 \text{ has } v_1, a_4 \text{ has } v_2), \text{ Court of Appeals, } v_2 > v_1, a_1 \text{ has } v_2, a_2 \text{ has } v_1, a_2 \text{ has Preponderance of Evidence, Context is Civil, } a_1 \text{ defeats } a_1, \text{ Something defeats } a_1, a_2 \text{ is justified.}\}
\]

For one final example, suppose a different hypothetical precedence *Vier v. Poster* which is much like *Wier v. Postal* except that it is decided in a Court of Appeals and the value ranking is \(v_1 > v_2\). Rather than Figure 12, we would have a graph with this one precedent which attacks all nodes with value ranking \(v_2 > v_1\) and all nodes with court at House of Lords. Where the case is presented at the Court of Appeals, even if the court desired to decide the case on the basis of value ranking \(v_2 > v_1\), it could not as the precedent asymmetrically attacks nodes with that ranking. In effect, the precedent imposes its value ranking on both the Crown Court and Court of Appeals, no matter what other value ranking those courts may desire. Thus, the preferred extension is:

\[
\{\text{Precedent(Court of Appeals, } v_1 > v_2, a_5 \approx a_1, a_6 \approx a_2, a_5 \text{ has } v_1, a_6 \text{ has } v_2), \text{ Crown Court, Court of Appeals, } v_1 > v_2, a_1 \text{ has } v_1, a_2 \text{ has } v_2, a_1 \text{ has Preponderance of Evidence, } a_2 \text{ has Preponderance of Evidence, Civil Procedure, } a_1 \text{ defeats } a_2, \text{ Something defeats } a_2, a_1 \text{ is justified.}\}
\]

### 4 Discussion

In this paper we have presented an approach to handling notions of judicial context in argumentation frameworks. Our approach introduces modes to represent concepts of the
legal domain and their relations in a structured argument network, so that we are able to explicitly express decisions for defeat of a claim relative to the assembly, values, value ranking, proof standards, and precedent. The current paper addresses several aspects of legal reasoning not accounted for in [9] since it adds a range of aspects which determine a decision.

Some previous research in AI and Law touches on issues related to our discussion. [29] takes into consideration the judicial hierarchy in making a decision on a claim. However, it is not set in an argumentation framework, but rather assigns aspects of a decision “points” which are summed, for example, the higher the court, the more the points. It does not consider the ways that courts have of establishing precedence, nor does it consider admissibility. In HYPO and CATO, well-known proposals on case-based reasoning ([23] and [24]), cases in the case base serve as precedents which bear on a current case. However, there is no representation of reasoning with the judicial hierarchy as all precedents have equal weight. Thus, determinations are not relativised to the different courts or procedural contexts.

We have illustrated our approach with three examples: appeals and social change which show precedence and precedent, and a change in the nature of proceedings which illustrates variable admissibility. In every case, however, we have restricted ourselves to a single conflict between a pair of arguments. To move to a more complete treatment of all aspects of judicial context we need to explore the following issues.

There are a range of interesting issues in legal reasoning which we have not addressed. For example, courts often are comprised of several judges who cast their decisions into majority and minority opinions. Recording the different opinions may be important for later judgements and so are worth recording. We have not represented this distinction as it does not effect decisions in a current case for the problems we are modeling. In addition, we have not represented lex specialis, which is the doctrine that a law governing a specific subject matter is not overridden by a law which only governs general matters. In our representation, this would mean that we would have to have some sort of “containment” relation between cases, where one is viewed as a more specific instance of another. If cases are presumed to subsume other cases, and if this information is included in the precedent relation, then this says that there is no attack of a more general on a more specific. This leaves unclear just what is the attack relation between them, if any. We would have two preferred extensions, each about a different “level” of the cases.

Finally, let us consider some concerns about our approach. One relates to complexity issues with respect to the number of nodes in the graph given conjunctions and perhaps disjunctions. We have used nodes which represent conjuncts as a convenience. Although there are potentially other conjunctions or even disjunctions that could be used as nodes, there is no requirement to use them, and so the potential for combinatorial explosion need not be realised. With respect to the number of values, we use only the pair-wise comparisons that emerge from the decisions we are considering. Therefore, although the number of possible specific audiences (i.e. total orderings on values) is the factorial of the number of values, we never need consider specific audiences, for example, suppose there are ten values, \( v_1, \ldots, v_{10} \), \( v_1 > v_2 \) subsumes all the audiences with
this preference [30]. A related issue is the usability of large graphs, which is beyond the scope of this paper and requires the development of user tools.

In this paper we have offered an analysis of precedent, precedence, and procedure using a refinement of abstract argumentation. The result is a set of substructures representing components which can be reused and refined with subsequent analysis of other cases or of more detailed legal systems. These substructures ensure that the argumentation framework as a whole will have the properties required to reason in accordance with the legal system modeled. It might be objected that a simpler approach would be to state the properties as, for example, integrity constraints. While this might allow the correct results it would hide the reasoning processes which we have made explicit. Thus, while constraints might seem a reasonable pragmatic choice in some applications, the situation is similar to the heuristics versus deep models debate for expert systems [31]. There the heuristics were generated from the deep model, the advantage being that the justification for the heuristics could be based on the deep model. Similarly we would argue that where justification of the observable features of the legal system or explicit reasoning is required, our analysis can play a significant role.

Other areas in which this line of research could be taken:

- Represent a body of case law such as in [9] by merging particular conflicts into cases, and cases into the corpus of decisions.
- Provide a range of sources of inadmissibility in addition to failure to meet the required PS. For example, evidence derived from illegal search and seizure may be legally inadmissible. This may require us to further articulate the A-to-I attacks with auxiliary arguments.
- Consider how an evidential status is determined.
- Incorporate into the analysis burden of proof [13], which relates participants in legal contexts to the argument network.

These are just several topics for future work in representing judicial context which have been beyond the reach of representation in AFs. Our approach offers great potential to provide a well-founded representation of arguments in legal case law as well as for other areas where contextual issues are crucial in determining the status of arguments.

References


Fig. 12. The Subgraphs Connected