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## Message authentication and hash functions

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## Message authentication

Message (or document) is **authentic** if

- It is genuine and
- came from its alleged source.

Message authentication is a **procedure** which verifies that received messages are authentic

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## Aspects of message authentication

We would like to ensure that

- The content of the message has not been changed;
- The source of the message is authentic;
- The message has not been delayed and replayed;

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## Message authentication techniques

- **Using conventional message encryption:**

if we assume that only sender and receiver share a secret key then the fact that receiver can successfully decrypt the message means the message has been encrypted by the sender

- **Without message encryption**

The message is not encrypted, but special authentication tag is generated and appended to the message. Generation of a tag is a much more efficient procedure than encryption of the message.

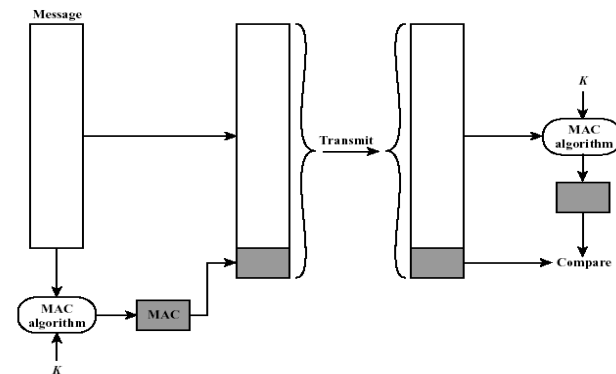
## Message Authentication Code

- Let  $A$  and  $B$  share a common secret key  $K$
- If  $A$  would like to send a message  $M$  to  $B$ , she calculates a message authentication code  $MAC$  of  $M$  using the key  $K$ :

$$MAC = F(K, M)$$

- Then  $A$  appends  $MAC$  to  $M$  and sends all this to  $B$ ;
- $B$  applies the  $MAC$  algorithm to the received message and compares the result with the received  $MAC$

## Message authentication using MAC



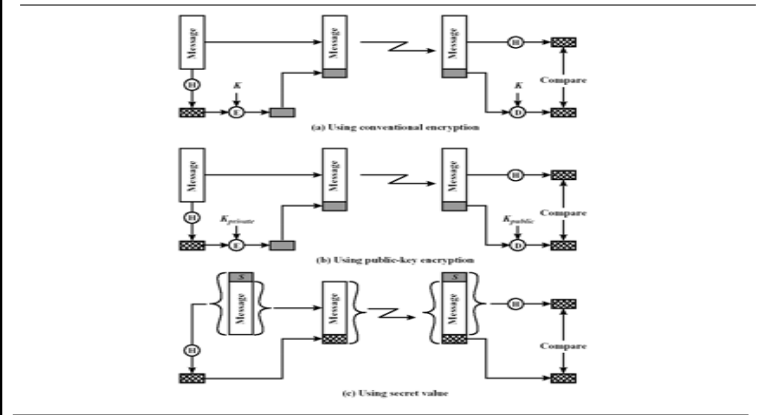
## MAC algorithms

- The process of MAC generation is similar to the encryption;
- The difference is a MAC algorithm need not be reversible → easier to implement and less vulnerable to being broken;
- Actually, standard encryption algorithms can be used for MAC generation:
  - For example, a message may be encrypted with DES and then last 16 or 32 bits of the encrypted text may be used as MAC

## One-way Hash functions

- An alternative method for the message authentication is to use one-way hash functions instead of MAC;
- The main difference is hash functions don't use a secret key:
$$h = H(M);$$
- “One-way” in the name refers to the property of such functions: they are easy to compute, but their reverse functions are very difficult to compute.

# Methods of authentication using hashes



# Hash function requirements

To be suitable for message authentication, the hash functions must have ideally the following properties:

- $H$  can be applied to a block of data of any size;
- $H$  produces a fixed-length output;
- $H(x)$  is easy to compute for any given  $x$ ;
- For any value  $h$  it is very difficult (infeasible) to compute  $x$  such that  $H(x)=h$  (**one-way property**);
- For any given  $x$ , it is very difficult (infeasible) to find  $y$  (not equal to  $x$ ) such that  $H(x) = H(y)$ ; (**weak collision resistance**);
- It is very difficult (infeasible) to find any pair  $(x,y)$  such that  $H(x) = H(y)$ ; (**strong collision resistance**).

# Simple hash function

- Let the input be a sequence of  $n$ -bit blocks
- Then simple hash function does bit-by-bit exclusive-OR (XOR) of every block

	bit 1	bit 2	...	bit n
block 1	$b_{11}$	$b_{21}$		$b_{n1}$
block 2	$b_{12}$	$b_{22}$		$b_{n2}$
	.	.	.	.
block m	$b_{1m}$	$b_{2m}$		$b_{nm}$
hash code	$C_1$	$C_2$		$C_n$

# Simple hash function

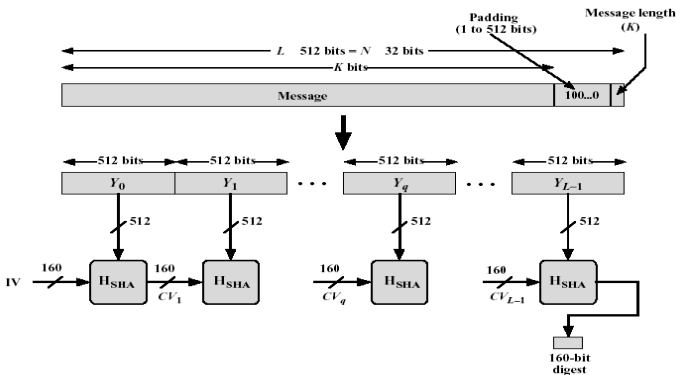
- Simple hash function does not satisfy **the weak (and strong) collision property**;
- for any message  $M$  it is very easy to generate a message  $M_1$  such that  $h(M) = h(M_1)$ :
  - Take arbitrary message  $M_2$ , compute  $h(M_2) = h_2$ , then
  - Add additional block to  $M_2$ , such that for the resulting  $M_3$  we have  $h(M_3) = h(M_1)$ .

# The SHA-1 Secure Hash Algorithm

## SHA-1 algorithm (1993-1995):

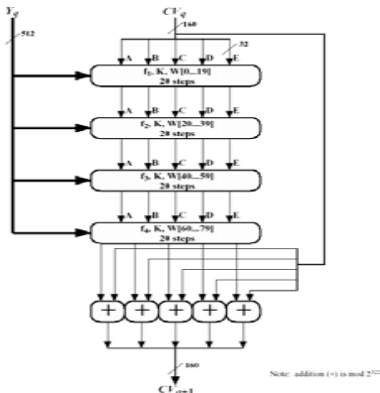
- It has been used in the sample program illustrating password-based encryption (practical sessions);
- Takes as input a message with a maximum length less than 2 to power 64 bits and produces as output a 160-bit message digest;
- The input is processed in 512-bit blocks;
- Each bit of the output is computed using all bits of the input.

# SHA-1 general scheme



# SHA-1 processing a single block

- The compression function;
- Includes 4 rounds with 20 steps each;
  - Each round takes the current 512-bits block and 160-bit buffer value and updates the content of the buffer.



# Other Secure Hash functions

	MD5	SHA-1	RIPEMD-160
Digest length	128 bits	160 bits	160 bits
Basic unit of processing	512 bits	512 bits	512 bits
Number of steps	64 (4 rounds of 16)	80 (4 rounds of 20)	160 (5 paired rounds of 16)
Maximum message size	$\infty$	$2^{64} - 1$ bits	$\infty$
Primitive logical functions	4	4	5
Additive constants used	64	4	9