

# A Framework for Mining Fuzzy Association Rules from Composite Items

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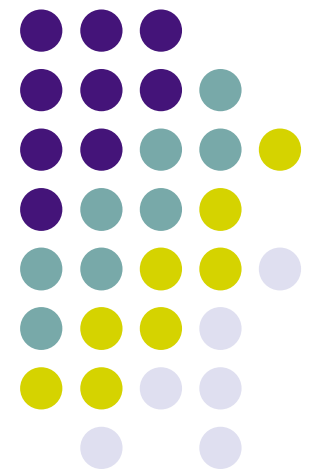
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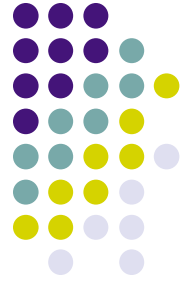




# Outline of the Presentation

Organised as follows:

- Introduction
  - Classical Association Rule Mining (ARM)
  - Quantitative Association Rule Mining
  - Fuzzy Association Rule Mining (FARM)
- Problem definition
- Methodology
- Example
- Conclusion & Further work



# Introduction

- **Association Rule Mining (ARM)**

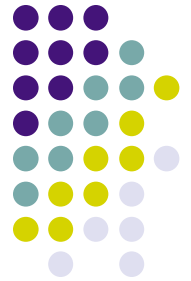
- Data Mining Technique for finding “interesting” patterns in binary valued data sets.
- Patterns usually translated into Association Rules (ARs) of the form

$$X \rightarrow Y$$

where X and Y are item sets.

- ARM algorithms usually operate using the support-confidence frame work, and utilise the Downward Closure Property (DCP) of itemsets.

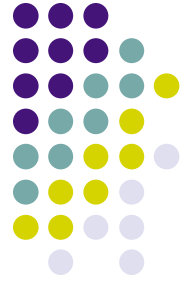
# Quantitative Association Rule Mining



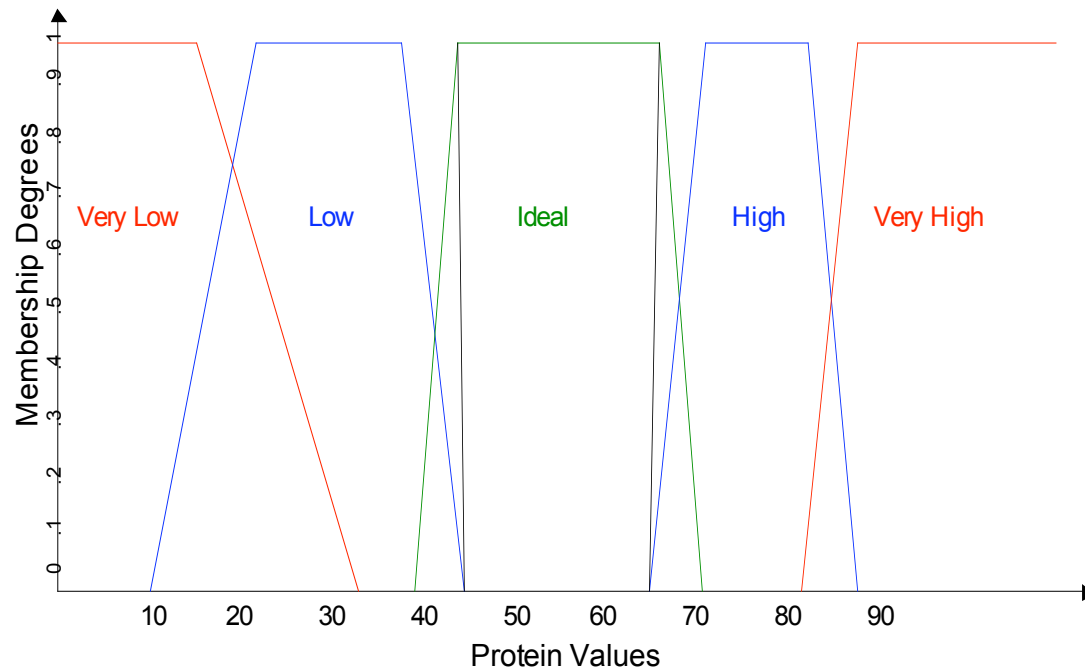
- **Quantitative ARM**

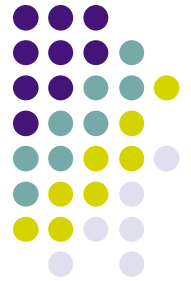
- Applied to non-boolean data.
- Data is discretized.
- In the case of numeric quantitative data items this causes what is known as the “crisp boundary” problem.

# Fuzzy Association Rule Mining (FARM)



- Fuzzy sets used to resolve the Crisp Boundary problem by providing a smooth change between boundaries.
- Fuzziness is defined by a membership mapping function.  
$$\mu(x) : A \rightarrow [0,1], x \in A$$
- Example (Trapezoidal membership function):

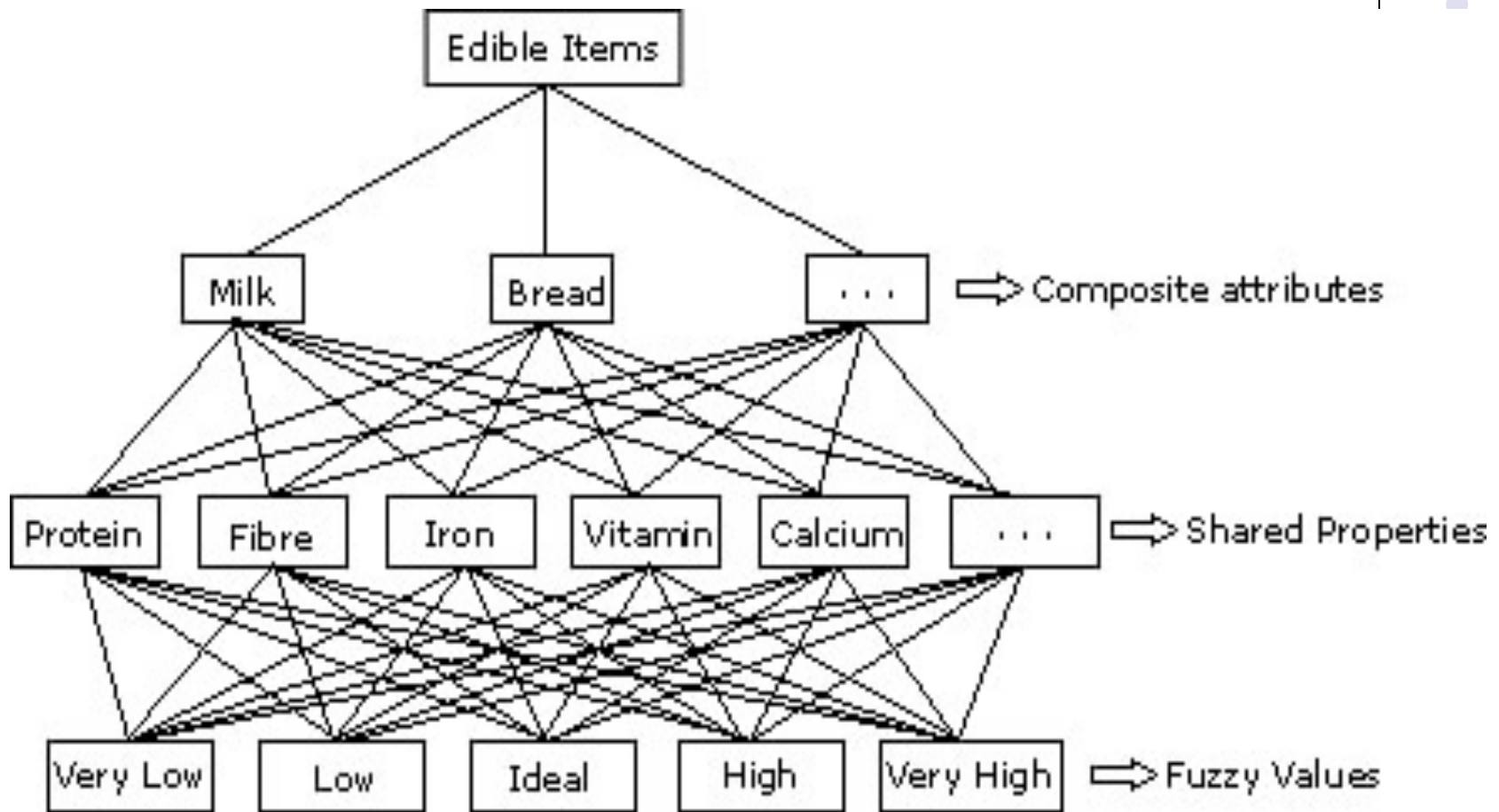
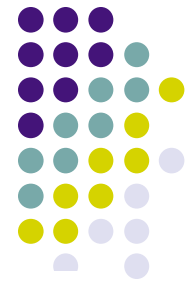


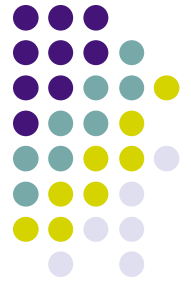


# FARM using composite attributes

- FARM extended to composite Attributes
- Composite Attributes
  - Objects (items) with collections of properties (set of values).
  - Properties can be quantitative or categorical.
  - Properties are shared across the attribute set.
  - Quantitative properties can be fuzzified into several ranges (fuzzy sets).

# FARM using composite attributes (Example)

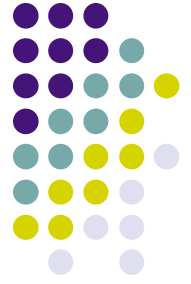




## Problem definition

- Given a Dataset  $D$  consisting of a set of transaction  $t = \{t_1, t_2, t_3, \dots, t_n\}$ , a set of composite items  $I = \{i_1, i_2, i_3, \dots, i_{|I|}\}$  and a set of properties  $P = \{p_1, p_2, p_3, \dots, p_m\}$ .
- Each transaction  $t_i$  is subset of  $I$ , and each item  $t_i[i_j]$  is a subset of  $P$ .
- Thus each item  $i_j$  will have associated with it a set of numeric values corresponding to the set  $P$ , i.e.  $t_i[i_j] = \{v_1, v_2, v_3, \dots, v_m\}$ .





# Problem Definition

- Example

TID	Record
1	{<a,{2,4,6}>, <b,{4,5,3}>}
2	{<c,{1,2,5}>, <d,{4,1,3}>}
3	{<a,{2,4,6}>, {<c,{1,2,5}>, <d,{4,1,3}>}
4	{<b,{4,5,3}>, <d,{4,1,3}>}

$$D=\{t_1, t_2, t_3, t_4\}$$

$$I=\{a, b, c, d\}$$

$$P=\{1, 2, 3, 4, 5, 6\}$$



# Problem Definition

- Property Dataset

- $D$  is initially transformed into a Property dataset  $D^P$ .
- $D^P$  consists of “Property Transactions”  $T^P = \{t^P_1, t^P_2, t^P_3, \dots, t^P_n\}$ .
- Each transaction  $t^P_i$ , is subset of  $P = \{p_1, p_2, p_3, \dots, p_m\}$ .
- The value for each Property attribute  $t^P_i[P_j]$  is obtained by summing the numeric values for all  $p_j$  in  $t_i$ . Thus

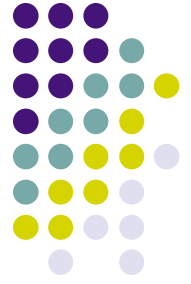
$$t^P_i[p_j] = \frac{\sum_{j=1}^{|t_i|} t^i[i_j[v_k]]}{|t_i|}$$



# Problem Definition

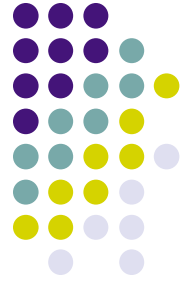
- Fuzzy Dataset

- $D^P$  is further transformed into a fuzzy dataset  $D'$ .
- A fuzzy dataset  $D'$  consists of fuzzy transactions  $T'=\{t'_1, t'_2, t'_3, \dots, t'_n\}$  and fuzzy property attributes  $P'$ .
- Each  $P'$  has a number of fuzzy sets associated with it, identified by a set of linguistic labels  $L=\{l_1, l_2, l_3, \dots, l_{|L|}\}$  e.g. {small, medium, large}.
- Each property attribute  $t^P_i[p_j]$  is associated (to some degree) with several fuzzy sets, with a membership degree in the range  $[0, 1]$ .
- Membership degree indicates the correspondence between the value of a given  $t^P_i[p_j]$  and the set of *fuzzy linguistic labels*.



# Problem Definition

- Composite Item Value Table
  - A composite item value table is a “look-up” table that allows us to get property values for specific items.
- Properties Table
  - A properties table is a table that maps all possible values for each property attribute  $t^P_i[P_j]$  onto fuzzy/overlapped ranges.



# Problem definition

- Fuzzy Normalisation Process (total membership degree value for properties to add up to 1)
  - The process of finding the contribution to the fuzzy support value,  $m'$ , for individual property attributes  $t'_i[p_j[l_k]]$  such that a partition of unity is guaranteed.

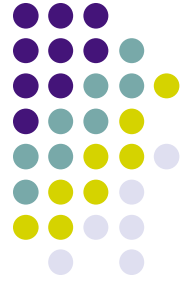
$$t'_i[p_j[l_k]] = \frac{\mu(t^p_i[p_j[l_k]])}{\sum_{x=1}^{|L|} \mu(t^p_i[p_j[l_x]])}$$

TID	VL	L	ID	H	VH	...
1	0.0	0.0	0.0	1.0	.32	...
2	.83	.38	0.0	0.0	0.0	...
3	...	...	...	...	...	...



TID	VL	L	ID	H	VH	...
1	0.0	0.0	0.0	.76	.24	...
2	.69	.31	0.0	0.0	0.0	...
3	...	...	...	...	...	...

# Problem definition



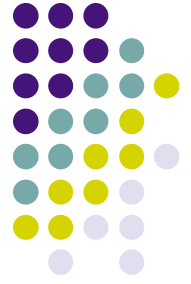
- Fuzzy Support
  - Fuzzy support is calculated as

$$FS(A) = \frac{\text{Sum of votes satisfying } A}{\text{Number of records in } T'}$$

$$\text{votes for } t_i \text{ satisfying } A = \sum_{i=1}^{i=n} \prod_{\forall [i[l]] \in A} t'[i_j[l_k]]$$

$$FS(A) = \frac{\sum_{i=1}^{i=n} \prod_{\forall [i[l]] \in A} t'[i_j[l_k]]}{n}$$

# Problem definition

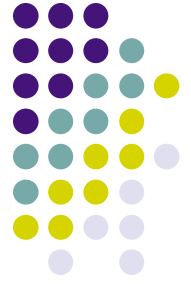


- Fuzzy Confidence

- Fuzzy confidence (FC) is calculated in the same manner that confidence is calculated in traditional ARM.
- Fuzzy confidence is calculated as:

$$FC(A \rightarrow B) = \frac{FS(A \cup B)}{FS(A)}$$

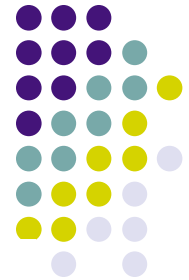
# Methodology



- **Data Transformation**
  - Transformation of raw dataset  $T$  into property dataset  $T^p$ .
  - Transformation of property dataset  $T^p$  into a database containing fuzzy extensions  $T'$ .
  - Normalization of fuzzy dataset.
  - Candidate Generation i.e. search for all fuzzy frequent itemsets that have support higher than user specified threshold.
  - Use frequent itemsets to generate all possible rules using fuzzy confidence or fuzzy correlation interestingness measures.



# Example Application



Nutrients/Fuzzy Ranges	Very Low			Low			Ideal			High			Very High						
	Min	Core	Max	Min	Core	Max	Min	Core	Max	Min	Core	Max	Min	Core					
Fiber	0	1	10	15	10	15	20	25	20	25	30	35	30	33	38	39	35	40	...
Iron	0	.6	8	12	8	12	16	18	16	18	19	20	19	20	22	23	22	23	...
Protein	0	1	15	30	10	20	35	40	35	40	60	65	60	65	75	80	75	70	...
VitaminaA	0	15	150	200	150	200	300	400	300	350	440	500	440	490	550	600	550	600	...
Zinc	0	.8	8	10	8	10	15	20	15	20	30	40	30	40	46	50	46	50	...
	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...

(a) Raw data ( $T$ )

TID	Items
1	X, Z
2	Z
3	X, Y, Z
4	...

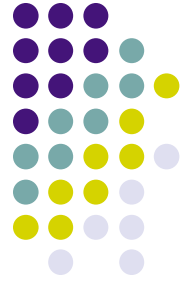
(b) Property data set ( $T^P$ )

TID	Pr	Fe	Ca	Cu
1	45	150	86	28
2	9	0	47	1.5
3	54	150	133	29.5
4	...	...	...	...

# Example Application

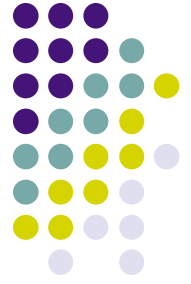


TID	Protein (Pr)					Iron (Fe)					...
	VL	L	Ideal	H	VH	VL	L	Ideal	H	VH	
1	0.0	0.7	0.3	0. 0	0.0	0.0	0.0	0.8	0.2	0.0	...
2	1.0	0.0	0.0	0. 0	0.0	1.0	0.0	0.0	0.0	0.0	...
3	0.0	0.0	0.9	0. 1	0.0	0.0	0.0	0.8	0.2	0.0	...
4	...	...	...	...	...	...	...	...	...	...	...



# Experimental Results

- Some example fuzzy rules produced by our approach (30% support, 50% confidence and 25% correlation) are as follows:
  - IF *Protein* intake is *Ideal* THEN *Carbohydrate* intake is *low*.
  - IF *Protein* intake is *Low* THEN *Vitamin A* intake is *High*.
  - IF *Protein* intake is *High* AND *Vitamin A* intake is *Low* THEN *Fat* intake is *High*.
- It is suggested that these rules are useful in analysing customer buying behavior concerning their nutrition.



# Conclusion & Further Work

- We have presented an approach for extracting hidden information from composite items.
- We showed that with such items, common properties can be defined as quantitative itemsets themselves, which are transformed into fuzzy sets.
- Overall, the approach presented is effective and efficient for analysing databases with composite items.
- Further work will evaluate our approach on real and larger datasets and compare real performance with other common fuzzy ARM algorithms.
- There is potential to apply this to other applications with composite items or attributes even with varying fuzzy sets between attributes e.g. image analysis and inventory control database.
- We are expanding our work with the possibilities to extend it for Fuzzy Utility and Weighted Association Rule Mining.