

Algorithmic Verification of Population Protocols

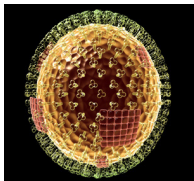
Othon Michail
Joint work with:
Ioannis Chatzigiannakis
Paul Spirakis

Research Academic Computer Technology Institute (RACTI)

SSS 2010
September 2010



Monitoring Cows' Health

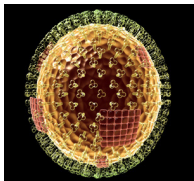


- Equip each cow in a heard with a sensor detecting influenza
- The sensor gives output 1

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- Question: Are there at least 5 infected cows?
- A solution:
 - The base station informs all agents to sense their environment
 - When 2 cows come close to each other their agents interact
 - The initiator takes the sum of the values and the responder takes 0
 - If a sum reaches 5 the output value 1 is propagated, otherwise forever remains 0

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Outstanding Properties of PPs

[AADFP '04]

The agents

- have constant memory (**uniformity**)
- do not have uids (**anonymity**)
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A Correct Population Protocol

- **Input alphabet** $X = \{0, 1\}$
- **Output alphabet** $Y = \{0, 1\}$
- **Set of states** $Q = \{q_0, q_1, \dots, q_5\}$
- **Input function** $I : X \rightarrow Q$, defined as $I(\sigma) = q_\sigma$,
- **Output function** $O : Q \rightarrow Y$, defined as $O(q_5) = 1$ and $O(q) = 0$ for all $q \in Q - \{q_5\}$
- **Transition function** δ :

$$\begin{aligned}(q_i, q_j) &\rightarrow (q_{i+j}, q_0), \text{ if } i + j < 5 \\ &\rightarrow (q_5, q_5), \text{ otherwise}\end{aligned}$$

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The Code

	q_0	q_1	q_2	q_3	q_4	q_5
q_0	(q_0, q_0)	(q_1, q_0)	(q_2, q_0)	(q_3, q_0)	(q_4, q_0)	(q_5, q_5)
q_1	(q_1, q_0)	(q_2, q_0)	(q_3, q_0)	(q_4, q_0)	(q_5, q_5)	(q_5, q_5)
q_2	(q_2, q_0)	(q_3, q_0)	(q_4, q_0)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)
q_3	(q_3, q_0)	(q_4, q_0)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)
q_4	(q_4, q_0)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)
q_5	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)

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	q_0	q_1	q_2	q_3	q_4	q_5
q_0	(q_0, q_0)	(q_1, q_0)	(q_2, q_0)	(q_3, q_0)	(q_4, q_0)	(q_5, q_5)
q_1	(q_1, q_0)	(q_2, q_0)	(q_3, q_0)	(q_4, q_0)	(q_5, q_5)	(q_5, q_5)
q_2	(q_2, q_0)	(q_3, q_0)	(q_4, q_0)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)
q_3	(q_3, q_0)	(q_4, q_0)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)	(q_5, q_5)
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- 400 cows are all sick
- It is possible that 100 agents go to q_4 and the rest to q_0
- But now the farmer will never be alarmed of the problem (alarm state q_5 never appears)
- Interestingly, the protocol also has an erroneous computation for only 8 cows

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- We want to **algorithmically verify our protocols** in order to avoid such total or partial failures, particularly in **critical applications**

Problem (*GBPVER*)

Given a population protocol \mathcal{A} for the basic model for which $Y_{\mathcal{A}} = \{0, 1\}$ and a first-order logical formula ϕ in Presburger arithmetic representing the *specifications* of \mathcal{A} determine whether \mathcal{A} *conforms* to ϕ .

- **Conforms** : For any input assignment x , and no matter how the computation proceeds, an **output-stable** configuration is eventually reached under which all agents output $\phi(x)$

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BPVER

- We mainly focus on the somewhat easier *BPVER* problem:
 - An integer $n \geq 2$ is also provided as part of the input
 - Here we want to determine whether \mathcal{A} conforms to ϕ on K_n (complete communication digraph of n agents)
- Since a computation is infinite and there is a finite number of configurations, at least one configuration appears infinitely often
 - It is known [AADFP '06] that those configurations form a final strongly connected component of the transition graph $G(\mathcal{C}, E)$, where \mathcal{C} is the set of all configurations and $(c, c') \in E$ iff $c \rightarrow c'$, e.g.

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 - An integer $n \geq 2$ is also provided as part of the input.
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- Since a computation is infinite and there is a finite number of configurations, at least one configuration appears infinitely often.
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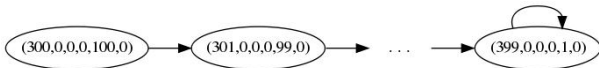


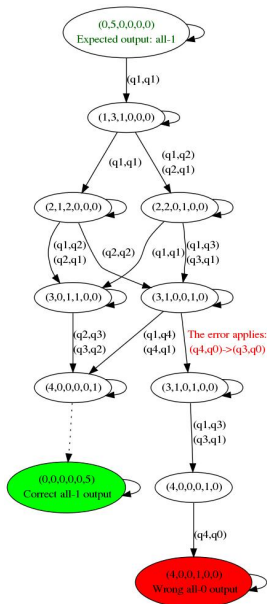
Figure: $(c_i)_{i=0,\dots,5}$, c_i denotes the number of agents in state q_i

Another Typo

	q_0	q_1	q_2	q_3	q_4	q_5
q_0	(q_0, q_0)	(q_1, q_0)	(q_2, q_0)	(q_3, q_0)	(q_4, q_0)	(q_5, q_5)
q_1	(q_1, q_0)	(q_2, q_0)	(q_3, q_0)	(q_4, q_0)	(q_5, q_5)	(q_5, q_5)
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- It should be $(q_4, q_0) \rightarrow (q_4, q_0)$ instead, because now one counter is decreased without a reason

Another Typo: $(q_4, q_0) \rightarrow (q_3, q_0)$



Hardness of *BPVER*

Theorem

BPVER is coNP-hard.

- The reduction is from *HAMPATH* (directed)
- Given $\langle D, s, t \rangle$
- We construct a protocol \mathcal{A} that does not conform to $(N_x < 0)$ on K_n iff D contains a directed hamiltonian path from s to t
- Also return $n = k - 1$, where $k = |V(D)|$
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- We construct a protocol \mathcal{A} that does not conform to $(N_x < 0)$ on K_n iff D contains a directed hamiltonian path from s to t
- Also return $n = k - 1$, where $k = |V(D)|$
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Hardness of *BPVER*

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BPVER is coNP-hard.

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- The protocol tries to **verify** whether its input assignment is a **legal hamiltonian path**
- If it encounters some violation, it **rejects** (otherwise, remains to an accepting output)
- Obviously
 - If $D \notin \text{HAMPATH}$ then no input assignment is a hamiltonian path and the protocol conforms to ϕ (always finds some violation and rejects)
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Theorem

GBPVER is coNP-hard.

- *BBPIVER* problem:
 - X is restricted to $\{0, 1\}$
 - a specific input assignment is provided as part of the input
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- **The bad news:** even for this restricted version, **hardness insists**
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Protocol Correctness Criteria

- 1 $\phi(c) = -1$ for some $c \in C_I$
- 2 $\exists c, c' \in C_I$ such that $c \xrightarrow{*} c'$ and $\phi(c) \neq \phi(c')$
- 3 $\exists c \in C_I$ and $c' \in C_F$ such that $c \xrightarrow{*} c'$ and $O(c') = -1$
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An Exponential Algorithm for *BPVER*

- Find the **reachable portion** of the transition graph
 - To find the initial configurations we can use Fenichel's algorithm [1968] for finding the **distributions of indistinguishable objects (agents) into distinguishable slots (initial states)**
- Partition the induced graph into its **strongly connected components** by e.g. Tarjan's algorithm [1972]
- Replace each component with a node to obtain a dag
- Initial strongly connected component: contains at least one initial configuration
 - 0-initial: all its initial configurations expect the all-0 output
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- There are easily checkable **criteria** for determining correctness
- Checking any of these defines a **possibly non-complete verifier**
- Checking 3 of these defines a **complete verifier**
- All of them are exponential since they are based on **searching the transition graph**
- We have implemented the **first verification tool for population protocols**
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Some Thoughts

- Can we avoid searching the huge transition graph by somehow **looking inside the protocol**?
- There is a **constructive proof** [AADFP '06] that a semilinear predicate is stably computable by the basic model
 - Unfortunately, there exists an unbounded number of correct protocols for the same predicate (we can simply add an unbounded number of dummy states and transitions)
 - e.g. replace $(q_0, q_1) \rightarrow (q_1, q_0)$ with

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 - e.g. replace $(q_0, q_1) \rightarrow (q_1, q_0)$ with

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$$(q_{d_1}, q) \rightarrow (q_{d_2}, q)$$

⋮

$$(q_{d_t}, q) \rightarrow (q_0, q)$$

Some Thoughts

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Some Thoughts

- Can we somehow compare the default protocol (given by the constructive proof) with the provided one?
 - Possibly by truncating the unnecessary states
- Design verifiers that are **not based on transition graph searching**
- For noncomplete communication graphs, protocols with stabilizing inputs [AACFJP '05], MPPs [CMS '09] and protocols using non-constant space (PM protocols) [CMNPS '10] we **do not have such constructive proofs**
- Study verification of protocols in these models
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FRONTS & VITRO

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Thank You!